

PRAAYAS

JEE 2026

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Mathematics

Trigonometric Functions

Lecture -02

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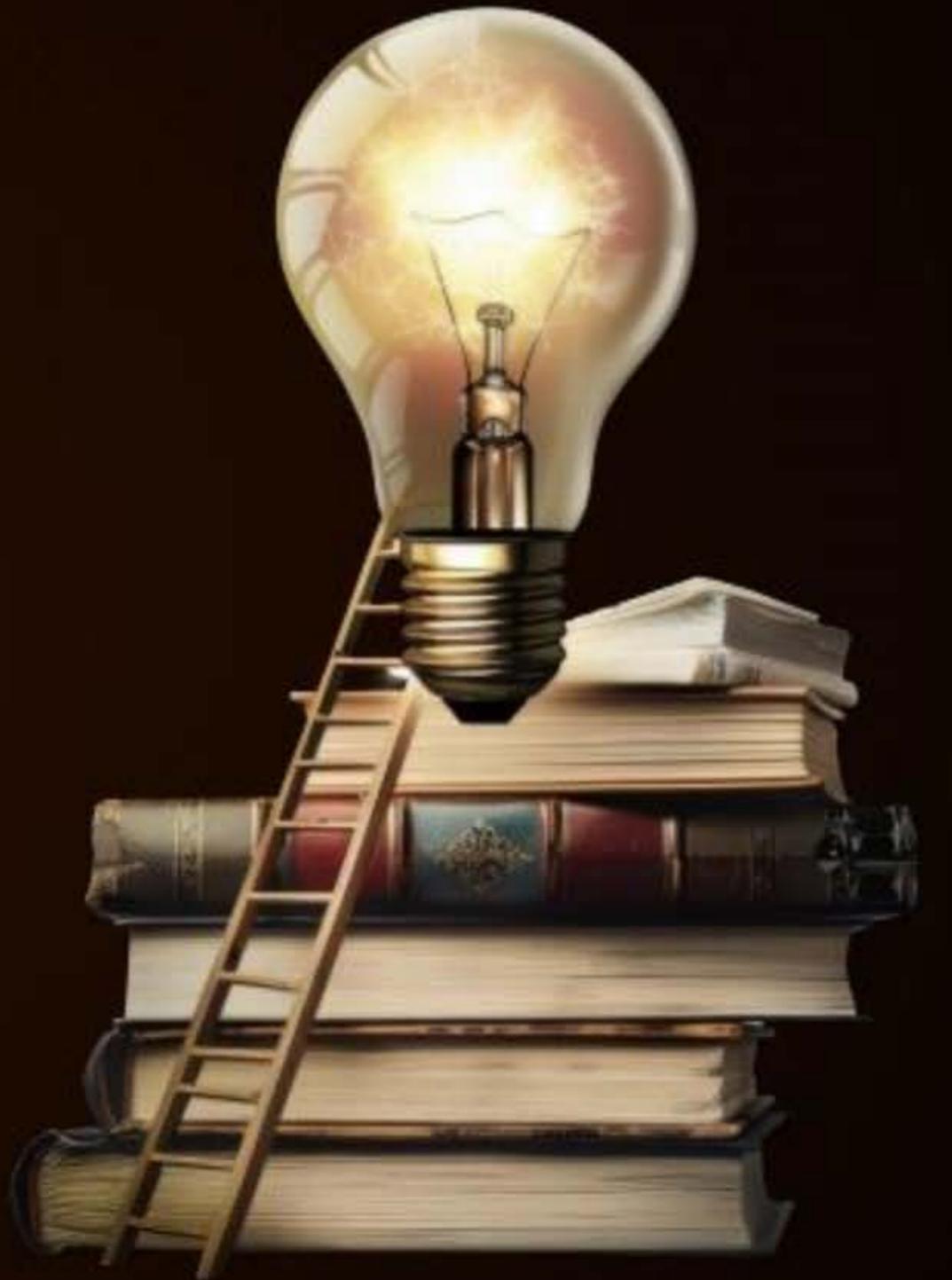


Topics *To be covered*



A Reduction Formula

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Recap of previous lecture



1. If for two positive numbers a & b we have

$a, A_1, A_2, \dots, A_n, b$ are in A.P.

$a, G_1, G_2, \dots, G_n, b$ are in G.P.

$a, H_1, H_2, \dots, H_n, b$ are in H.P.

then $A_1 \geq G_1 \geq H_1$, $A_2 \geq G_2 \geq H_2$, $A_n \geq G_n \geq H_n$

also $A_1 H_n = A_2 H_{n-1} = A_3 H_{n-2} = \dots = A_n H_1 = ab$

2. $2x + 3y = 5$ then minimum value of $x^2 + y^2 = \underline{\frac{25}{13}}$.

3. $a + b + c + d = 1$ then $\sqrt{a} + \sqrt{b} + \sqrt{c} + \sqrt{d} \leq \underline{2}$

$$\textcircled{2} \quad 2, 3, x, y \in \mathbb{R}$$

By CS Ineq

$$(2x + 3y)^2 \leq (2^2 + 3^2)(x^2 + y^2)$$

$$25 \leq 13(x^2 + y^2)$$

$$x^2 + y^2 \geq \frac{25}{13}$$



$a + b + c + d = 1$
 $1, 1, 1, 1, \sqrt{a}, \sqrt{b}, \sqrt{c}, \sqrt{d} \in \mathbb{R}$

M(1)
 $\sqrt{a} + \sqrt{b} + \sqrt{c} + \sqrt{d} \Big|_{\max} = 2$
By CS inequality

$$(1 \cdot \sqrt{a} + 1 \cdot \sqrt{b} + 1 \cdot \sqrt{c} + 1 \cdot \sqrt{d})^2 \leq (1^2 + 1^2 + 1^2 + 1^2) (\sqrt{a}^2 + \sqrt{b}^2 + \sqrt{c}^2 + \sqrt{d}^2)$$

$$(\sqrt{a} + \sqrt{b} + \sqrt{c} + \sqrt{d})^2 \leq 4 \cdot 1$$

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$$\sqrt{a} + \sqrt{b} + \sqrt{c} + \sqrt{d} \leq 2$$

M(2)

using RMS \geq A.M

$$\sqrt{\frac{\sqrt{a}^2 + \sqrt{b}^2 + \sqrt{c}^2 + \sqrt{d}^2}{4}} \geq \frac{\sqrt{a} + \sqrt{b} + \sqrt{c} + \sqrt{d}}{4}$$

$$\frac{1}{2} = \sqrt{\frac{a+b+c+d}{4}} \geq \frac{\sqrt{a} + \sqrt{b} + \sqrt{c} + \sqrt{d}}{4}$$

$$\sqrt{a} + \sqrt{b} + \sqrt{c} + \sqrt{d} \leq 2 \text{ Ans}$$

Recap *of previous lecture*



Tan!@

4. If $a + b + c = 1$ & $a, b, c > 0$ then the minimum value of $a^2 + 2b^2 + c^2$ is _____

5. $\sec x - \tan x$ & $\sec x + \tan x$ are reciprocal of each other.

6. $\operatorname{cosec} 30^\circ + \sec 60^\circ + \tan \frac{\pi}{4} + \cot^2 \frac{\pi}{3} = \underline{2+2+1+\frac{1}{3} = 16/3}$

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7. $\tan 90^\circ$ is N.D $\cot 90^\circ$ is 0

$\operatorname{cosec} 0^\circ$ is N.D $\cot 0^\circ$ is N.D

$\sec 90^\circ$ is N.D



Homework Discussion

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QUESTION

(RPP 1)



Paragraph

Consider the quadratic equation $2x^2 - (4m + 2)x + m^2 + m = 0, m \in \mathbb{R}$

1. The number of positive integer values of 'm' such that the equation has exactly one root in (2, 3) is

(A) 3

(B) 4

(C) 5

(D) 6

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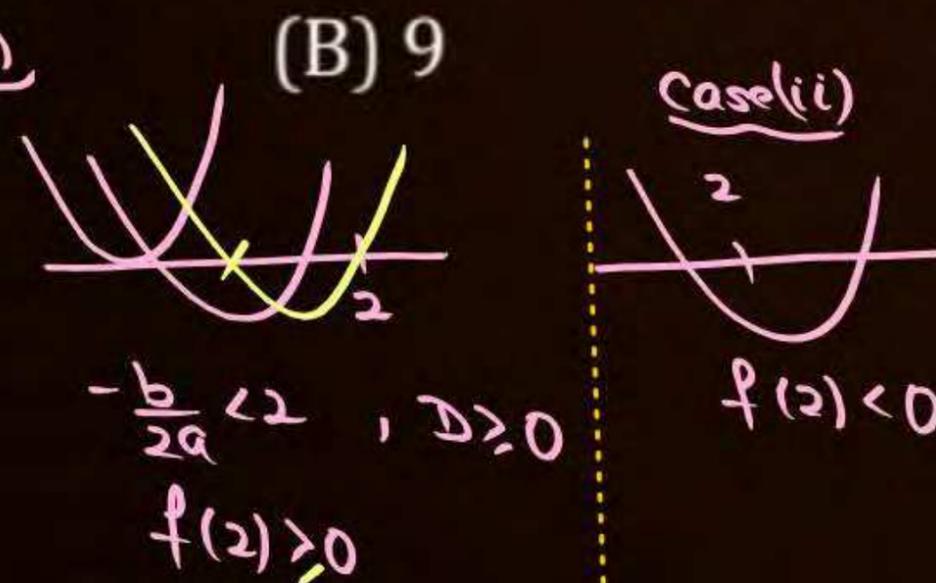
2. The number of negative integral values of 'm' such that $m > -10$ and at least one root of the equation is smaller than '2' is

(A) 8

(B) 9

(C) 6

(D) 4



Ans. (1) B, (2) B

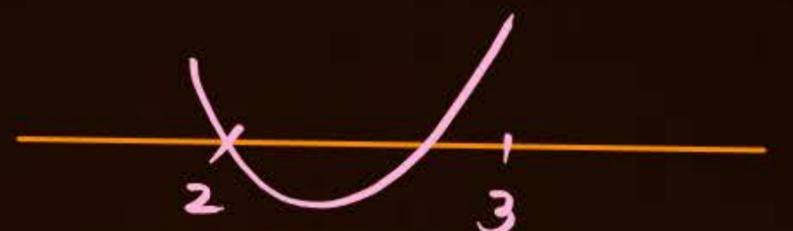


Q1. case (i)



$$f(2) \cdot f(3) < 0$$

case (ii)



case (iii)



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QUESTION

(Challenger Problem (Answers Sahi hai))



If $ax^2 + bx + c = 0, a \neq 0, a, b, c \in \mathbb{R}$ has two distinct real roots in $(1, 2)$ then

- ~~A~~ (a) $(5a + 2b + c) > 0$
- ~~B~~ (a) $(5a + 2b + c) < 0$
- ~~C~~ $2a + b > 0$
- ~~D~~ (a) $(4a + 2b + c) > 0$

RPP 02



© $1 < -\frac{b}{2a} < 2$

$1 + \frac{b}{2a} < 0$

$\frac{2a+b}{2a} < 0$

$\begin{cases} a > 0 \\ 2a+b < 0 \end{cases} \quad \begin{cases} a < 0 \\ 2a+b > 0 \end{cases}$

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$a \neq 0$
 $a f(1) > 0$
 $a f(2) > 0 \Rightarrow a(4a + 2b + c) > 0$

Now $a(5a + 2b + c)$
 $= a(a + 4a + 2b + c)$
 $= a^2 + a(4a + 2b + c) > 0$
 $\quad \quad \quad > 0 \quad \quad \quad > 0$

Ans. A, D



$$\begin{array}{l}
 1 < \alpha, \beta < 2 \\
 \swarrow \quad \searrow \\
 \alpha + \beta > 2 \quad \alpha + \beta < 4 \\
 \downarrow \\
 -\frac{b}{a} > 2 \\
 \alpha + \frac{b}{a} < 0 \\
 \frac{2a+b}{a} < 0 \\
 \underbrace{\quad \quad \quad}_a \\
 \begin{array}{l}
 a < 0 \quad \quad a > 0 \\
 \swarrow \quad \searrow \\
 2a+b > 0 \quad 2a+b < 0
 \end{array}
 \end{array}$$

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Trigonometry



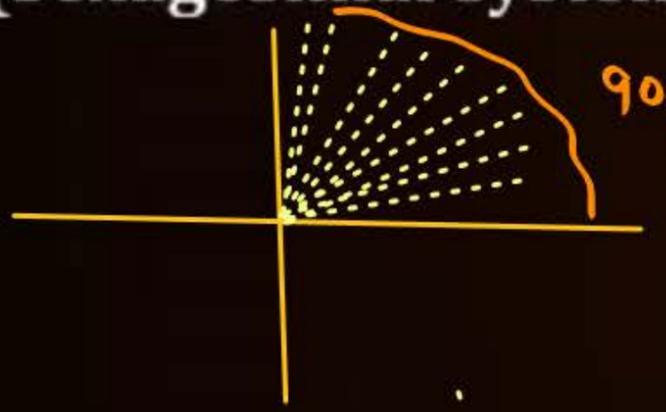
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Trigonometry



System of measurement of angle

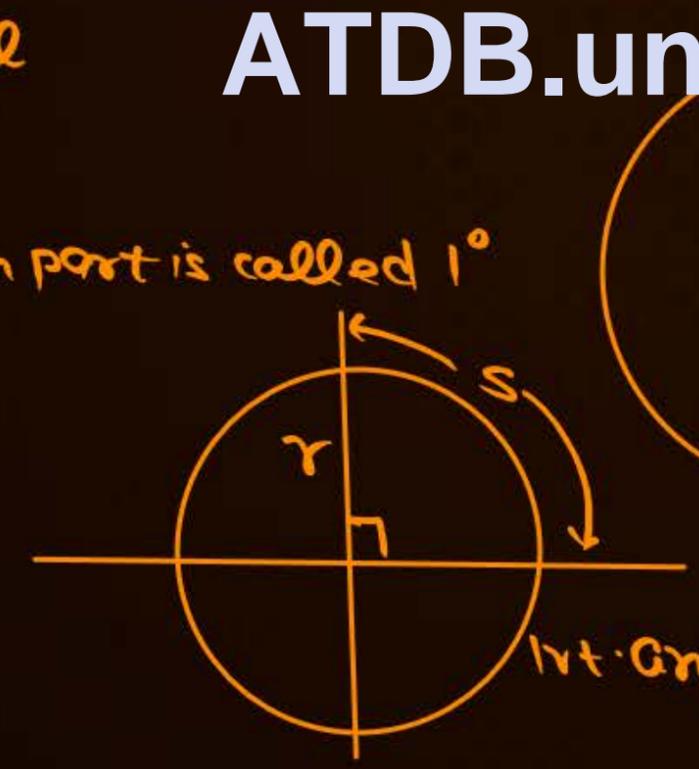
Degree
(Sexagesimal system)



90 equal parts

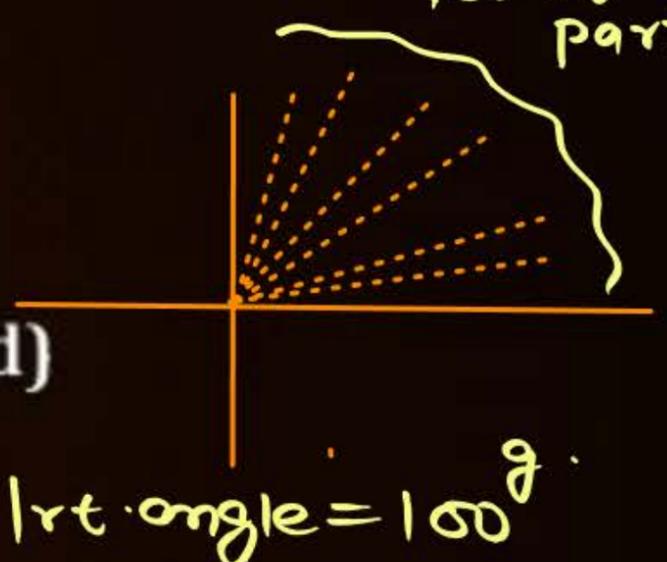
Each part is called 1°

Radian
(Circular system)



$$\text{Rt. Angle} = \frac{s}{r} = \frac{2\pi r}{4} = \frac{\pi}{2}$$

French
(not in used)



Each part is called 1 grade
100 equal parts

Rt. angle = 100^g

$$\theta^s = \frac{s}{r} \text{ dimensionless.}$$

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$$\text{1 rt angle} = 90^\circ = \left(\frac{\pi}{2}\right)^c = 100^g.$$

$$90^\circ = \left(\frac{\pi}{2}\right)^c$$

$$1^\circ = \left(\frac{\pi}{180}\right)^c = 0.0175^c$$

$$1^c = \left(\frac{180}{\pi}\right)^\circ = 57.3^\circ$$

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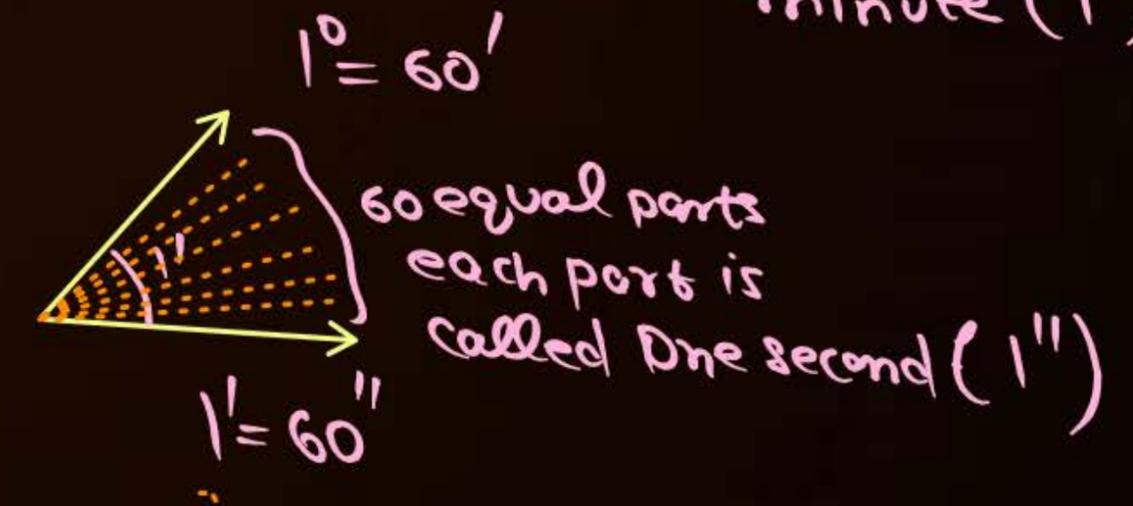
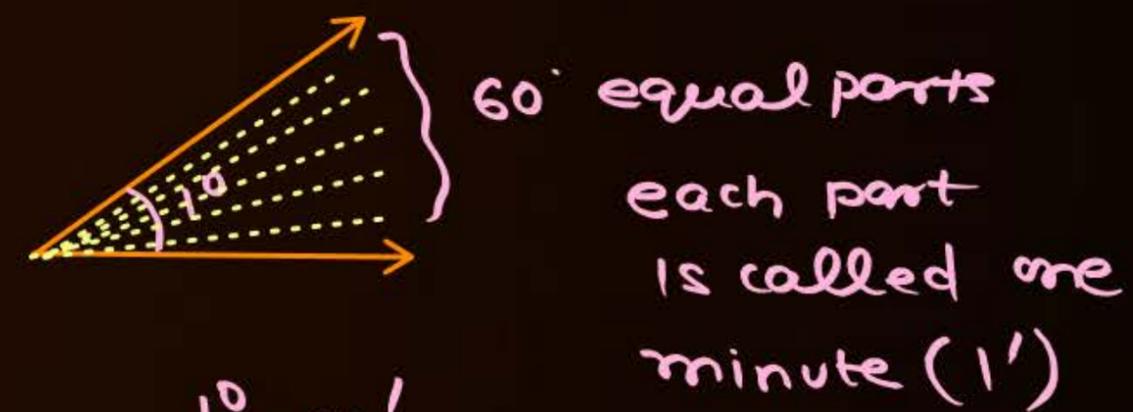
$$\begin{aligned} \star \theta^\circ &= \left(\frac{\pi}{180} \cdot \theta\right)^c \\ \star \theta^c &= \left(\frac{180}{\pi} \theta\right)^\circ \end{aligned}$$



Yaad Rakho

- * $\frac{\pi}{6} = 30^\circ$
- * $\frac{\pi}{3} = 60^\circ$
- * $\frac{7\pi}{6} = 210^\circ$
- * $\frac{5\pi}{3} = 300^\circ$
- * $\frac{\pi}{4} = 45^\circ$
- * $\frac{\pi}{2} = 90^\circ$
- * $\frac{4\pi}{3} = 240^\circ$
- * $\frac{7\pi}{4} = 315^\circ$
- * $\frac{\pi}{12} = 15^\circ$
- * $\frac{2\pi}{3} = 120^\circ$
- * $\frac{5\pi}{4} = 225^\circ$
- * $2\pi = 360^\circ$
- * $\frac{\pi}{15} = 12^\circ$
- * $\frac{3\pi}{4} = 135^\circ$
- * $\frac{3\pi}{2} = 270^\circ$
- * $\frac{\pi}{10} = 18^\circ$
- * $\frac{5\pi}{6} = 150^\circ$
- * $\frac{11\pi}{6} = 330^\circ$
- * $\frac{\pi}{8} = 22.5^\circ$
- * $\frac{3\pi}{8} = 67.5^\circ$
- * $\frac{5\pi}{12} = 75^\circ$

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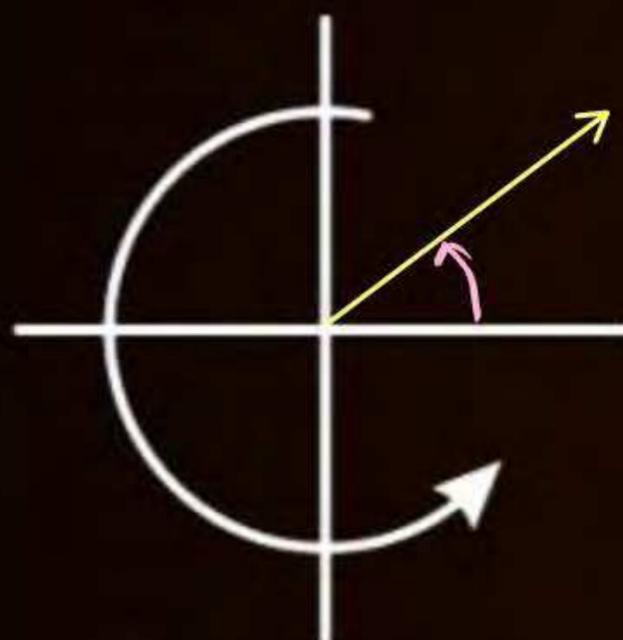




Measurement of Angle



Sign Convention:



Anticlockwise direction
will indicate +ve angle

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Clockwise direction
will indicate -ve angle



Angles at Boundaries of Quadrants



$$5 + (n-1)4 = 4n + 1$$

T_{-2} ↓ $-\frac{7\pi}{2}$, T_{-1} ↓ $-\frac{3\pi}{2}$, T_0 ↓ $\frac{\pi}{2}$, T_1 ↓ $\frac{5\pi}{2}$, T_2 ↓ $\frac{9\pi}{2}$ --- $(4n+1)\frac{\pi}{2}$

$(2n+1)\pi$
 $-\dots -3\pi, -\pi, \pi, 3\pi, 5\pi -\dots$
 (odd π)

$-\dots -4\pi, -2\pi, 0, 2\pi, 4\pi, 6\pi -\dots$
 (Even π) $(2n\pi)$

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$-\dots -\frac{5\pi}{2}, -\frac{\pi}{2}, \frac{3\pi}{2}, \frac{7\pi}{2}, \frac{11\pi}{2} -\dots$
 $(4n-1)\frac{\pi}{2}$

$n \in I$



$$27 = 6 \times 4 + 3$$

$$= 6 \times 4 + 4 - 1$$

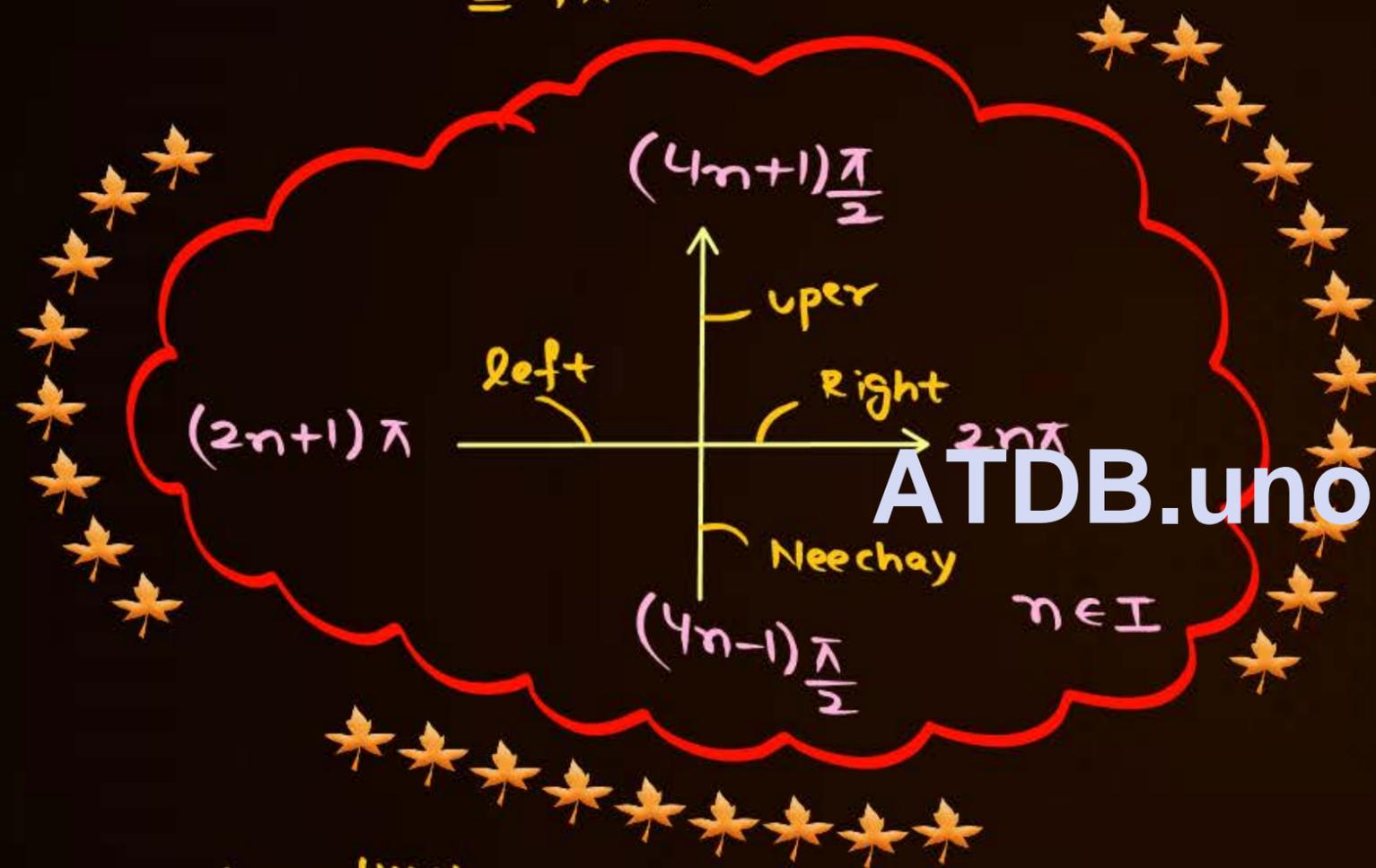
$$= 7 \times 4 - 1$$

$$65 = 4 \times 16 + 1$$

$$4 \overline{) 25}^6$$

$$\underline{24}$$

$$1$$



★ $2025 \frac{\pi}{2}$ — $(4n+1) \frac{\pi}{2}$ type

↓
uper

★ $2027 \frac{\pi}{2}$

$(4n-1) \frac{\pi}{2}$ type

↓
Neechay.

$$4 \overline{) 27}^6$$

$$\underline{24}$$

$$3$$

$$27 = 4 \cdot 7 - 1$$

$$47 = 4 \times 12 - 1$$

★ $5047 \frac{\pi}{2}$ — $(4n-1) \frac{\pi}{2}$ (Neechay)

★ $2025\pi \rightarrow$ left

★ $1065 \frac{\pi}{2}$ — $(4n+1) \frac{\pi}{2}$ (uper)

$$47 = 4 \times 11 + 3$$

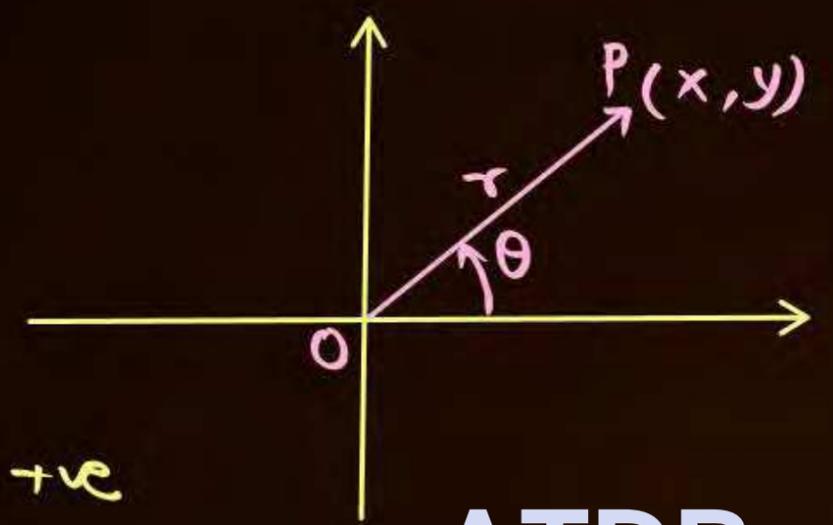
$$= 4 \times 11 + 4 - 1$$

$$= 4 \times (11 + 1) - 1$$

$$= 4 \times 12 - 1$$



Real definition of 2 basic functions (Sine & Cosine)



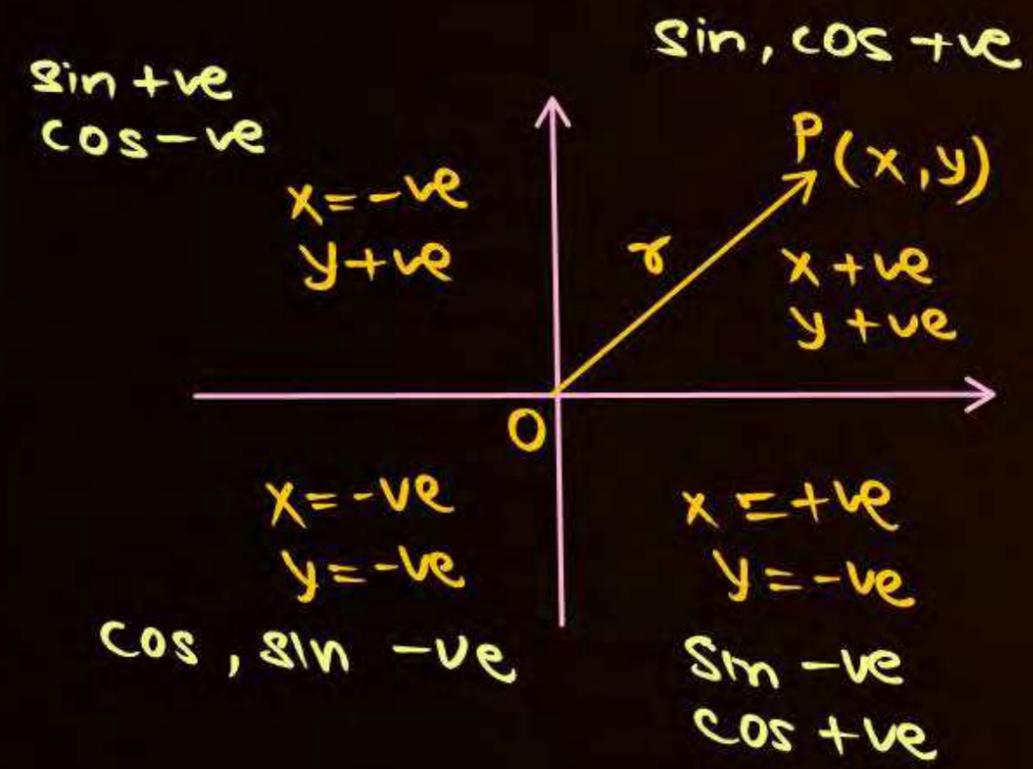
* $\sin \theta = \frac{y \text{ coord of } P}{\text{length of } OP} = \frac{y}{r}$

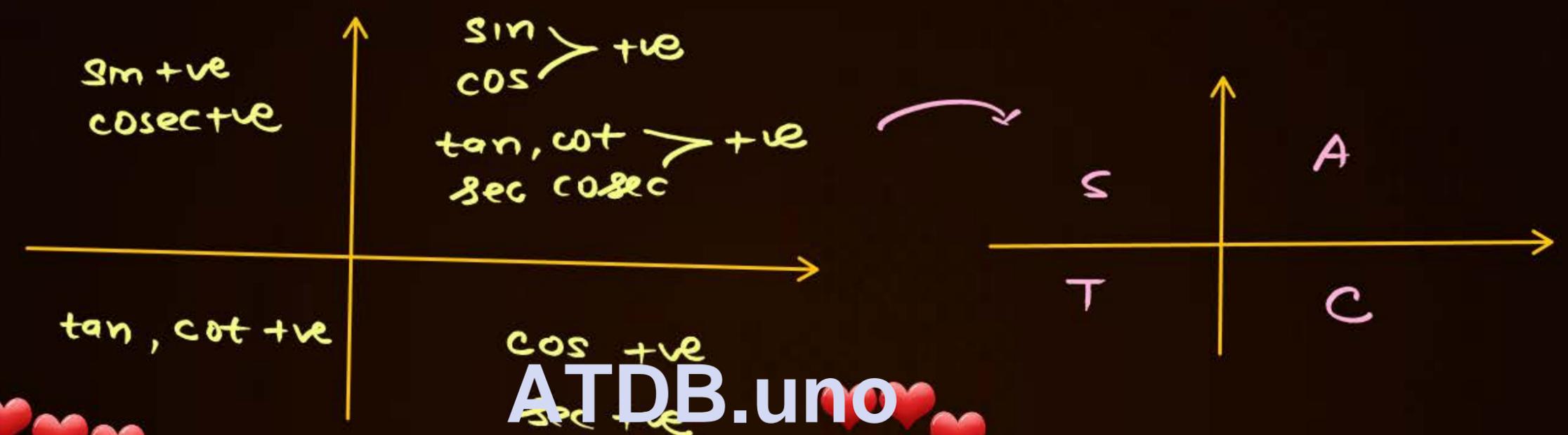
* $\cos \theta = \frac{x \text{ coord of } P}{\text{length of } OP} = \frac{x}{r}$

* $\tan \theta = \frac{y}{x}$ * $\cot \theta = \frac{x}{y}$

* $\sec \theta = \frac{r}{x}$ * $\csc \theta = \frac{r}{y}$

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$$n\pi \cup (2n+1)\pi/2$$

$$\equiv \frac{n\pi}{2}$$

$$* 2n\pi \cup (2n+1)\pi = n\pi$$

$$* (4n+1)\frac{\pi}{2} \cup (4n-1)\frac{\pi}{2} = (2n+1)\frac{\pi}{2}$$

$$-\frac{3\pi}{2}, -\frac{\pi}{2}, \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \frac{7\pi}{2}$$

$$-\frac{7\pi}{2}, -\frac{3\pi}{2}, \frac{\pi}{2}, \frac{5\pi}{2}, \frac{9\pi}{2}, -\frac{\pi}{2}, \frac{3\pi}{2}, \frac{7\pi}{2}$$



Value of T-Ratios at Boundaries of Quadrants



$$\sin(2n+1)\pi = 0$$

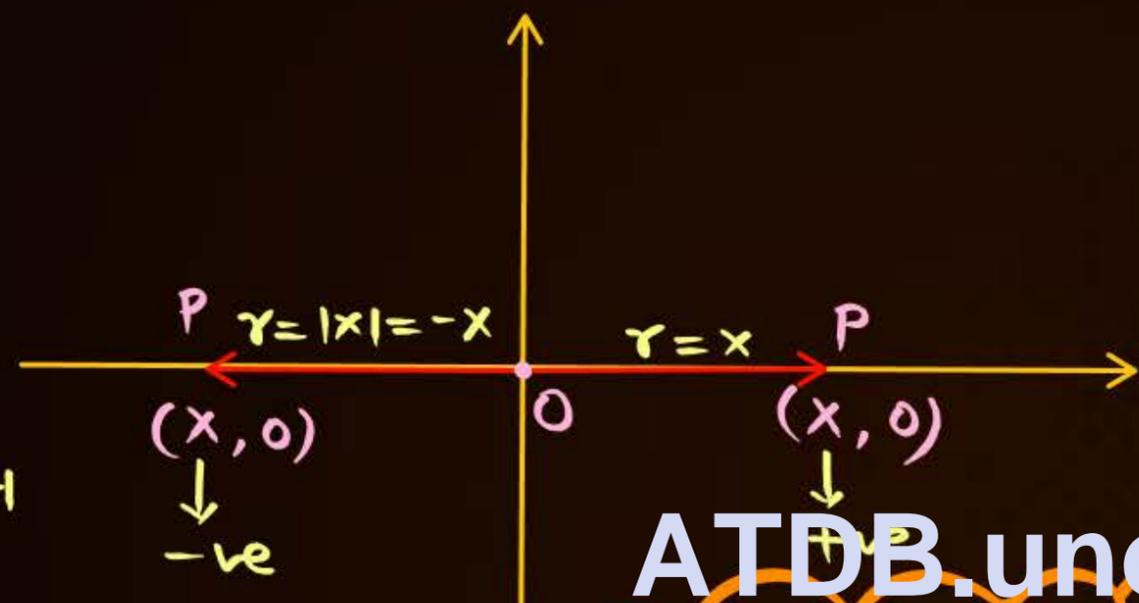
$$\cos(2n+1)\pi = \frac{x}{y} = -1$$

$$\tan(2n+1)\pi = 0$$

$$\sec(2n+1)\pi = -1$$

$$\cot(2n+1)\pi \text{ N.D.}$$

$$\operatorname{cosec}(2n+1)\pi \text{ N.D.}$$



$$\sin 2n\pi = \frac{0}{y} = 0$$

$$\cos 2n\pi = \frac{x}{y} = 1$$

$$\tan 2n\pi = 0$$

$$\sec 2n\pi = 1$$

$$\operatorname{cosec} 2n\pi \text{ N.D.}$$

$$\cot 2n\pi \text{ N.D.}$$

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$$\star \sin \theta = 0 \Leftrightarrow \theta = n\pi$$

$$\star \tan \theta = 0 \Leftrightarrow \theta = n\pi$$

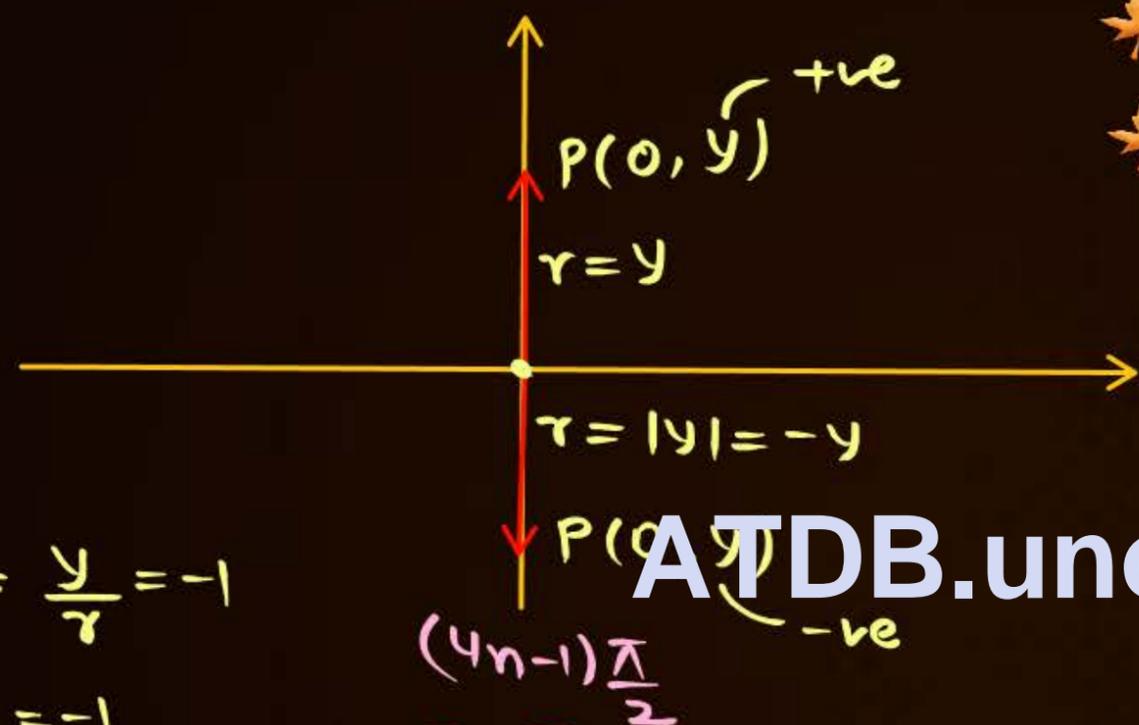
$$\star \sec \theta, \cos \theta = 1 \Leftrightarrow \theta = 2n\pi$$

$$\star \sec \theta, \cos \theta = -1 \Leftrightarrow \theta = (2n+1)\pi$$

$\star \cot \theta, \operatorname{cosec} \theta$ are not defined for $n\pi$



Value of T-Ratios at Boundaries of Quadrants



$$\sin(4n-1)\frac{\pi}{2} = \frac{y}{r} = -1$$

$$\operatorname{cosec}(4n-1)\frac{\pi}{2} = -1$$

$$\cos(4n-1)\frac{\pi}{2} = \frac{0}{r} = 0$$

$$\sec(4n-1)\frac{\pi}{2} = \text{N.D.}$$

$$\tan(4n-1)\frac{\pi}{2} = \text{N.D.}$$

$$\cot(4n-1)\frac{\pi}{2} = 0$$

$$\star \sin(4n+1)\frac{\pi}{2} = \frac{y}{r} = 1$$

$$\star \cos(4n+1)\frac{\pi}{2} = \frac{0}{r} = 0$$

$$\tan(4n+1)\frac{\pi}{2} = \text{N.D.}$$

$$\cot(4n+1)\frac{\pi}{2} = 0$$

$$\sec(4n+1)\frac{\pi}{2} = \text{N.D.}$$

$$\operatorname{cosec}(4n+1)\frac{\pi}{2} = 1$$

$$\star \operatorname{cosec}\theta, \sin\theta = 1 \Leftrightarrow \theta = (4n+1)\frac{\pi}{2}$$

$$\star \operatorname{cosec}\theta, \sin\theta = -1 \Leftrightarrow \theta = (4n-1)\frac{\pi}{2}$$

$$\star \cos\theta = 0 \Leftrightarrow \theta = (2n+1)\frac{\pi}{2}$$

$$\star \tan\theta, \sec\theta \text{ are N.D. at } \theta = (2n+1)\frac{\pi}{2}$$

$$\star \cot\theta = 0 \Leftrightarrow \theta = (2n+1)\frac{\pi}{2}$$



$$\tan \theta, \sin \theta = 0 \iff \theta = n\pi$$

$$\sec \theta, \cos \theta = 1 \iff \theta = 2n\pi$$

$$\sec \theta, \cos \theta = -1 \iff \theta = (2n+1)\pi$$

$$\cos \theta = \pm 1 \iff \theta = n\pi$$

$\cot \theta, \operatorname{cosec} \theta$ are not defined at $\theta = n\pi$

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$$\sin \theta, \operatorname{cosec} \theta = 1 \iff \theta = (4n+1)\frac{\pi}{2}$$

$$\sin \theta, \operatorname{cosec} \theta = -1 \iff \theta = (4n-1)\frac{\pi}{2}$$

$$\cos \theta = 0 \iff \theta = (2n+1)\frac{\pi}{2}$$

$\tan \theta, \sec \theta$ are not defined at $\theta = (2n+1)\frac{\pi}{2}$

$$\cot \theta = 0 \iff \theta = (2n+1)\frac{\pi}{2}$$

QUESTION



If $a = \cos(2012\pi)$, $b = \sec(2013\pi)$ and $c = \tan(2014\pi)$ then

A $a < b < c$

~~**B** $b < c < a$~~

C $c < b < a$

D $a = b < c$

$$a = \cos(2012\pi) = 1$$

$$b = \sec(2013\pi) = -1$$

$$c = \tan(2014\pi) = 0$$

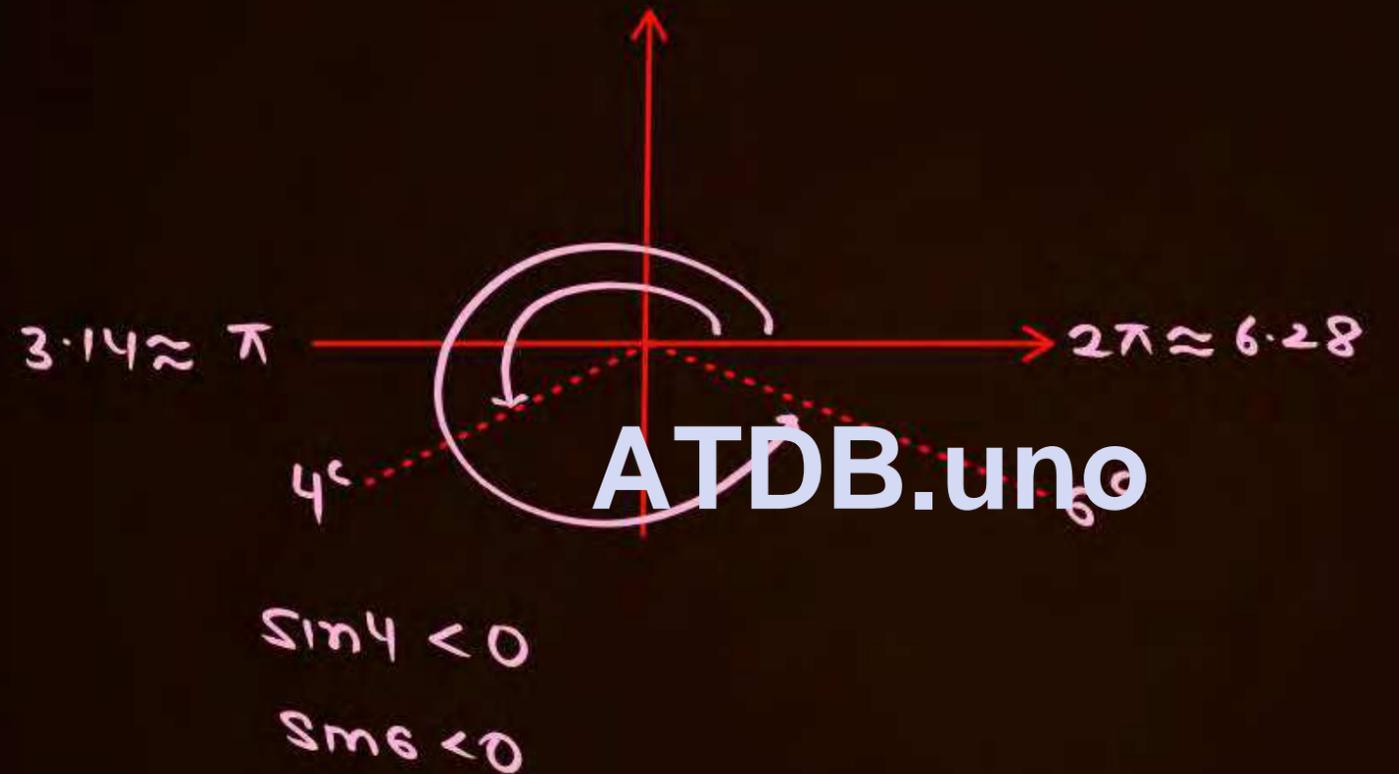
$$a > c > b.$$

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QUESTION



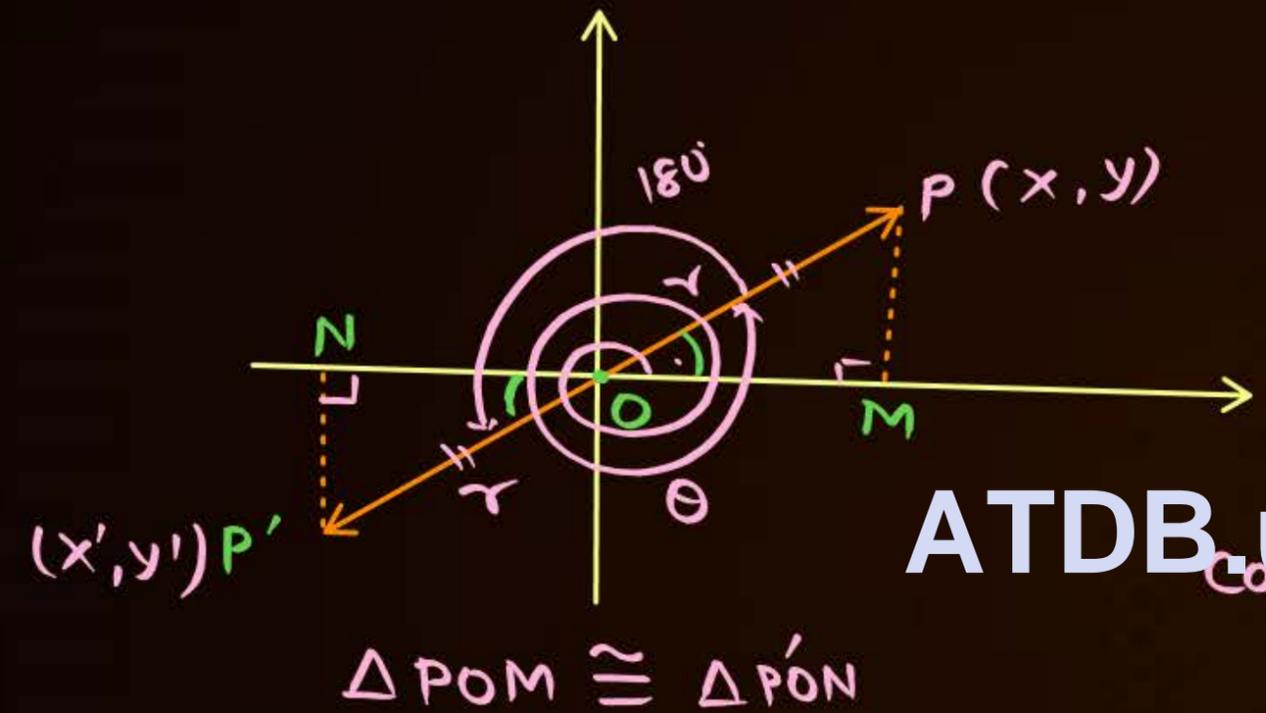
$\frac{\sin 4}{\sin 6}$ is negative. **T/F**





Reduction Formulae

used for finding T-ratios of larger Angles



$$\sin(180^\circ + \theta) = \frac{y'}{r} = -\frac{NP'}{r} = -\frac{MP}{r} = -\frac{y}{r}$$

$$\sin(180^\circ + \theta) = -\frac{y}{r} = -\sin \theta$$

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$$\cos(180^\circ + \theta) = \frac{x'}{r} = -\frac{ON}{r} = -\frac{OM}{r} = -\frac{x}{r} = -\cos \theta$$

$\Delta POM \cong \Delta P'ON$

$NP' = MP$
 $ON = OM$ (CPCT)

- ★ $\sin(180^\circ + \theta) = -\sin \theta$
- ★ $\cos(180^\circ + \theta) = -\cos \theta$
- ★ $\tan(180^\circ + \theta) = \tan \theta$
- ★ $\cot(180^\circ + \theta) = \cot \theta$
- ★ $\operatorname{cosec}(180^\circ + \theta) = -\operatorname{cosec} \theta$
- ★ $\sec(180^\circ + \theta) = -\sec \theta$



Reduction Formulae

used for finding T-ratios of larger Angles



$$25 = 6 \times 4 + 1$$

$$5 = 4 \times 1 + 1$$

$$27 = 4 \times 7 - 1$$

change ↴
 sin ↔ cos
 tan ↔ cot
 sec ↔ cosec

No change

No change

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* $\sin\left(\frac{3\pi}{2} + \theta\right) = -\cos\theta$

* $\cos\left(2025\frac{\pi}{2} + \theta\right) = -\sin\theta$
 (4n+1) $\frac{\pi}{2}$ type

* $\tan\left(5\frac{\pi}{2} - \theta\right) = \cot\theta$

* $\cot\left(2027\frac{\pi}{2} + \theta\right) = -\tan\theta$

change ↴
 sin ↔ cos
 tan ↔ cot
 sec ↔ cosec

$\sin(5000\pi + \theta) = +\sin\theta$

$\cos(2521\pi - \theta) = -\cos\theta$

* $\sin\left(\frac{\pi}{2} + \theta\right) = +\cos\theta$ (sth)

* $\tan\left(\frac{\pi}{2} + \theta\right) = -\cot\theta$

* $\sin(\pi - \theta) = +\sin\theta$ (sth)

* $\sin(2\pi - \theta) = -\sin\theta$



Reduction Formulae



x	$\frac{\pi}{2} - \alpha$	$\frac{\pi}{2} + \alpha$	$\pi - \alpha$	$\pi + \alpha$	$\frac{3\pi}{2} - \alpha$	$\frac{3\pi}{2} + \alpha$	$2\pi - \alpha$
$\sin x$	$\cos \alpha$	$\cos \alpha$	$\sin \alpha$	$-\sin \alpha$	$-\cos \alpha$	$-\cos \alpha$	$-\sin \alpha$
$\cos x$	$\sin \alpha$	$-\sin \alpha$	$-\cos \alpha$	$-\cos \alpha$	$-\sin \alpha$	$\sin \alpha$	$\cos \alpha$
$\tan x$	$\cot \alpha$	$-\cot \alpha$	$-\tan \alpha$	$\tan \alpha$	$\cot \alpha$	$-\cot \alpha$	$-\tan \alpha$
$\cot x$	$\tan \alpha$	$-\tan \alpha$	$-\cot \alpha$	$\cot \alpha$	$\tan \alpha$	$-\tan \alpha$	$-\cot \alpha$

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Reduction Formulae for $-\theta$

$$\begin{aligned} \cos(-\theta) &= \cos(2\pi + (-\theta)) & \sin(-\theta) &= \sin(2\pi + (-\theta)) \\ &= \cos(2\pi - \theta) & &= \sin(2\pi - \theta) \\ &= \cos\theta & &= -\sin\theta \end{aligned}$$

$$* \sin(-\theta) = -\sin\theta$$

$$* \cos(-\theta) = \cos\theta$$

$$* \tan(-\theta) = -\tan\theta$$

$$* \cot(-\theta) = -\cot\theta$$

$$* \operatorname{cosec}(-\theta) = -\operatorname{cosec}\theta$$

$$* \sec(-\theta) = \sec\theta$$

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$$\sin(2\pi + \theta) = \sin\theta$$

$$\cos(2\pi + \theta) = \cos\theta$$

$$\tan(2\pi + \theta) = \tan\theta$$

!



QUESTION



Find the value of

$$3 \overline{) 25} \\ \underline{24} \\ 1$$

(i) $\sin\left(\frac{25\pi}{3}\right)$

(ii) $\cos\left(\frac{41\pi}{4}\right)$

(iii) $\tan\left(\frac{-16\pi}{3}\right)$

(iv) $\cot\left(\frac{29\pi}{4}\right)$

$$\sin\left(8\pi + \frac{\pi}{3}\right) = + \sin \pi/3 = \frac{\sqrt{3}}{2}$$

$$\cos\left(10\pi + \frac{\pi}{4}\right)$$

$$- \tan \frac{16\pi}{3}$$

$$\cot\left(7\pi + \frac{\pi}{4}\right)$$

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$$= - \tan\left(5\pi + \frac{\pi}{3}\right)$$

$$= - \tan \pi/3 = -\sqrt{3}$$

$$\cot \pi/4$$

$$= 1$$

$$\checkmark \frac{1}{\cancel{2}}$$

QUESTION

$$+ 360^\circ$$

Find the value of

$$\sin(360^\circ + 45^\circ) = \sin 45^\circ = \frac{1}{\sqrt{2}}$$

(i) $\sin(405^\circ)$

(ii) $\sec(-1470^\circ)$

(iii) $\tan(-300^\circ)$

(iv) $\cot(585^\circ)$

TAH 1A
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$$\sec(1470^\circ) = \sec(4 \times 360^\circ + 30^\circ)$$

$$\downarrow 2\pi$$

$$\parallel \sec(8\pi + 30^\circ)$$

$$\parallel \sec 30^\circ = \frac{2}{\sqrt{3}}$$

$$360^\circ \overline{) 1470^\circ} \\ \underline{1440} \\ 30^\circ$$



QUESTION



Express in terms of ratios of a positive angle, which is less than 45° , the quantities.

- (i) $\cos 1410^\circ$ (ii) $\cot(-1054^\circ)$ (iii) $\operatorname{cosec}(-756^\circ)$

$$\begin{array}{l}
 \begin{array}{r}
 360^\circ \overline{) 1410} \\
 \underline{1080} \\
 330
 \end{array} \\
 \cos(4 \times 360^\circ - 30^\circ) \\
 \cos(8\pi - 30^\circ) \\
 = \cos 30^\circ = \frac{\sqrt{3}}{2}
 \end{array}$$

$$\begin{array}{l}
 \cos(360^\circ \times 3 + 330^\circ) \\
 \parallel \\
 \cos(6\pi + 330^\circ) \\
 \parallel \\
 \cos 330^\circ \\
 \cos(360^\circ - 30^\circ) \\
 \cos 30^\circ = \frac{\sqrt{3}}{2}
 \end{array}$$

TAH 1B

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QUESTION



TAH 2

Fill in the rest of the blanks yourself.

$\angle A$	0°	30°	45°	60°	90°	120°	135°	150°	180°	210°	225°	240°	270°	300°	315°	330°	360°
$\sin A$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1												
$\cos A$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0												
$\tan A$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	ND												
$\operatorname{cosec} A$	ND	2	$\sqrt{2}$	$2\sqrt{3}$	1												
$\sec A$	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	ND												
$\cot A$	ND	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}}$	0												

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$$\theta \in (0, \pi/4) \quad * \sin \theta < \cos \theta$$

$$* \tan \theta < \cot \theta$$

$$\theta \in (\pi/4, \pi/2) \quad * \cos \theta < \sin \theta$$

$$* \cot \theta < \tan \theta$$

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QUESTION



What sign has $\sin A - \cos A$ for the following values of A?

(i) 215°

$$\begin{aligned} \sin 215^\circ - \cos 215^\circ &= \sin(180^\circ + 35^\circ) - \cos(180^\circ + 35^\circ) \\ &= -\sin 35^\circ + \cos 35^\circ \\ &= \cos 35^\circ - \sin 35^\circ = +ve \end{aligned}$$



$$\cos 35^\circ > \sin 35^\circ$$

(ii) -634°

$$\begin{aligned} \sin(-634^\circ) - \cos(-634^\circ) &= -\sin 634^\circ - \cos 634^\circ \\ &= -\sin(720^\circ - 86^\circ) - \cos(720^\circ - 86^\circ) \end{aligned}$$

$$\begin{aligned} &= -\sin(4\pi - 86^\circ) - \cos(4\pi - 86^\circ) \\ &= -(-\sin 86^\circ) - (+\cos 86^\circ) \\ &= \sin 86^\circ - \cos 86^\circ = +ve \end{aligned}$$

$$\begin{array}{r} \sqrt{720} \\ 634 \\ \hline 86 \end{array}$$



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QUESTION**TAH 3**

What sign has $\sin A + \cos A$ for the following values of A ?

(i) 278°

(ii) -1125°

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QUESTION**TAH 4A**

Find the value of

(i) $\operatorname{cosec}(-750^\circ)$

(ii) $\cos(-2220^\circ)$

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QUESTION

TAH 4B



$\sin 420^\circ \cos 390^\circ + \cos (-300^\circ) \sin (-330^\circ)$ equals

A 0

B 1

C -1

D 2

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QUESTION



TAH 4C

Find the value of

(i) $\sec\left(-\frac{19\pi}{3}\right)$

(ii) $\operatorname{cosec}\left(-\frac{33\pi}{4}\right)$

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ASNC (Nayi Soch)



$$\sin(\pi - \theta) = \sin \theta$$

$$\tan(\pi - \theta) = -\tan \theta$$

$$\cos(\pi - \theta) = -\cos \theta$$

$$\cot(\pi - \theta) = -\cot \theta$$

$$\operatorname{cosec}(\pi - \theta) = \operatorname{cosec} \theta$$

$$\operatorname{sec}(\pi - \theta) = -\operatorname{sec} \theta$$

$$\begin{aligned} & \sin(180^\circ - 50^\circ) \\ &= \sin 50^\circ \end{aligned}$$

$\alpha + \beta = \pi$ i.e. α, β are supplementary

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$$\star \sin \alpha = \sin \beta, \operatorname{cosec} \alpha = \operatorname{cosec} \beta$$

$$\star \cos \alpha = -\cos \beta, \star \cot \alpha = -\cot \beta$$

↳ coz $\sin \alpha = \sin(\pi - \beta) = \sin \beta$

$$\star \tan \alpha = -\tan \beta, \star \operatorname{sec} \alpha = -\operatorname{sec} \beta$$



ASNC (Nayi Soch)



$$\text{if } \alpha + \beta = \frac{\pi}{2}$$

$$\star \sin \alpha = \cos \beta$$

$$\star \tan \alpha = \cot \beta$$

$$\star \sec \alpha = \csc \beta$$

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QUESTION



Evaluate :

$$\frac{\sin \frac{11\pi}{17} \cos \frac{10\pi}{13} \tan \frac{\pi}{7}}{\cos \frac{3\pi}{13} \sin \frac{6\pi}{17} \tan \frac{6\pi}{7}} = 1$$

Handwritten notes above the expression: $\frac{11\pi}{17} + \frac{6\pi}{17} = \pi$

(ii)

$$\frac{\sin \frac{\pi}{5} \cos \frac{7\pi}{9} \tan \frac{6\pi}{11}}{\cos \frac{2\pi}{9} \sin \frac{4\pi}{5} \tan \frac{5\pi}{11}} = 1$$

$$\frac{10\pi}{13} + \frac{3\pi}{13} = \pi \quad \frac{\pi}{7} + \frac{6\pi}{7} = \pi$$

$$\cos \frac{10\pi}{13} = -\cos \frac{3\pi}{13}$$

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QUESTION



Evaluate :

$$(iii) \frac{\overset{1}{\cancel{\sin \frac{\pi}{7}}} \overset{1}{\cancel{\cos \frac{5\pi}{11}}} \overset{-1}{\cancel{\tan \frac{3\pi}{7}}} = -1}{\cancel{\cos \frac{5\pi}{14}} \cancel{\sin \frac{\pi}{22}} \cancel{\tan \frac{4\pi}{7}}}$$

$$\frac{\pi}{7} + \frac{5\pi}{14} = \frac{7\pi}{14} = \pi/2$$

$$\frac{5\pi}{11} + \frac{\pi}{22} = \frac{11\pi}{22} = \pi/2$$

$$\frac{3\pi}{7} + \frac{4\pi}{7} = \pi$$

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QUESTION



$$\tan \frac{\pi}{11} + \tan \frac{2\pi}{11} + \tan \frac{4\pi}{11} + \tan \frac{7\pi}{11} + \tan \frac{9\pi}{11} + \tan \frac{10\pi}{11} \text{ equals}$$

$$\frac{\pi}{11} + \frac{10\pi}{11} = \pi$$

A 1

B -1

C 0

D 2

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QUESTION



$$\sin^2 \frac{\pi}{18} + \sin^2 \frac{\pi}{9} + \sin^2 \frac{7\pi}{18} + \sin^2 \frac{4\pi}{9} \text{ equals}$$

A 1

B -1

C 0

~~**D** 2~~

$$\cos^2 \frac{\pi}{9} + \cos^2 \frac{\pi}{18}$$

$$\frac{\pi}{18} + \frac{4\pi}{9} = \frac{9\pi}{18} = \frac{\pi}{2}$$

$$\frac{\pi}{9} + \frac{7\pi}{18} = \frac{2\pi + 7\pi}{18} = \frac{\pi}{2}$$

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QUESTION [JEE Mains 2024 (8 April)]



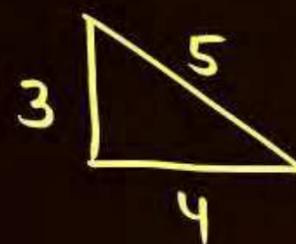
If $\sin x = -\frac{3}{5}$, where $\pi < x < \frac{3\pi}{2}$, then $80(\tan^2 x - \cos x)$ is equal to

~~A~~ 109

B 108

C 19

D 18



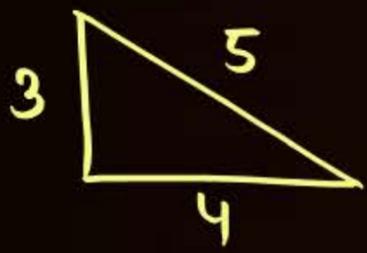
$$\sin x = -\frac{3}{5} \quad \text{sign bharo jao}$$

$$\tan x = +\frac{3}{4} \quad \tan^2 x = \frac{9}{16}$$

$$\cos x = -\frac{4}{5} \quad -\cos x = \frac{4}{5}$$

$$\tan^2 x - \cos x = \frac{9}{16} + \frac{4}{5} = \frac{45+64}{80}$$

$$80(\tan^2 x - \cos x) = 109.$$



$x \in \text{quad II or quad III}$

$$\cos x = -\frac{4}{5}$$

$$\tan x = -\frac{3}{4} \quad \text{or} \quad \tan x = \frac{3}{4}$$

$$\sin x = \frac{3}{5} \quad \downarrow \quad x \in \text{quad II}$$

$$\sin x = -\frac{3}{5} \quad \downarrow \quad x \in \text{quad III}$$

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$$\cos \theta = -\frac{4}{5} = \frac{x \cos x}{r}$$

$$x = -4 \quad \theta \in \text{II, III}$$

$$r = 5$$

$$r^2 = x^2 + y^2$$

$$25 = 16 + y^2$$

$$y = \pm 3$$

Quad III

$$\sin \theta = \frac{y}{r} = \frac{3}{5} \quad \text{or} \quad -\frac{3}{5}$$

$$\tan \theta = \frac{y}{x} = \frac{3}{-4} \quad \text{or} \quad \frac{-3}{-4}$$

Quad II



Sabse Important Baat



Sabhi Class illustrations Retry Karni hai

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Today's KTK



No Selection TRISHUL Selection with Good Rank
Apnao IIT Jao



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QUESTION

KTK 1



$$\frac{\tan(90^\circ - \theta) \sec(180^\circ - \theta) \sin(-\theta)}{\sin(180^\circ + \theta) \cot(360^\circ - \theta) \operatorname{cosec}(90^\circ - \theta)} \text{ equals}$$

- A** 1
- B** -1
- C** 0
- D** 2

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Ans. A

QUESTION

KTK 2



If ABCD is a quadrilateral, then show that

$$(a) \quad \cos \frac{B+C}{2} + \cos \frac{A+D}{2} = 0$$

$$(b) \quad \tan \frac{A+C}{4} = \cot \frac{B+D}{4}$$

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QUESTION

KTK 3



The value of $\cos^2 \frac{\pi}{16} + \cos^2 \frac{3\pi}{16} + \cos^2 \frac{5\pi}{16} + \cos^2 \frac{7\pi}{16}$ is

- A** 2
- B** 1
- C** 0
- D** None of these

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Ans. A

QUESTION [JEE Mains 2019]

KTK 4



Let $f_k(x) = \frac{1}{k} (\sin^k x + \cos^k x)$ for $k = 1, 2, 3, \dots$

Then for all $x \in \mathbb{R}$, the value of $f_4(x) - f_6(x)$ is equal to

- A** $\frac{5}{12}$
- B** $-\frac{1}{12}$
- C** $\frac{1}{4}$
- D** $\frac{1}{12}$

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Ans. D

QUESTION

KTK 5



If θ is the each interior angle of a regular dodecagon then the value of $\sin \theta + \cos \theta + \tan \theta + \cot \theta + \sec \theta + \operatorname{cosec} \theta$, is

- A** positive
- B** negative and less than (-1)
- C** zero
- D** negative and less than (-2)

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Ans. B

QUESTION

KTK 6



The value of $\sum_{n=0}^{1947} \frac{1}{2^n + \sqrt{2^{1947}}}$ is equal to

A $\frac{487}{\sqrt{2^{1945}}}$

B $\frac{1946}{\sqrt{2^{1947}}}$

C $\frac{1947}{\sqrt{2^{1947}}}$

D $\frac{1948}{\sqrt{2^{1947}}}$

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Ans. A

QUESTION

KTK 7



If $a, b, c \in \mathbb{R}^+$ then the minimum value of $a(b^2 + c^2) + b(c^2 + a^2) + c(a^2 + b^2)$ is equal to

- A** abc
- B** $2abc$
- C** $3abc$
- D** $6abc$

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Ans. D

QUESTION

KTK 8



The line $x + y = 1$ meets x -axis at A and y -axis at B , P is the mid-point of AB ;

P_1 is the foot of the perpendicular from P to OA ;

M_1 is that of P_1 from OP ;

P_2 is that of M_1 from OA ;

M_2 is that of P_2 from OP ;

P_3 is that of M_2 from OA ; and so on. **ATDB.uno**

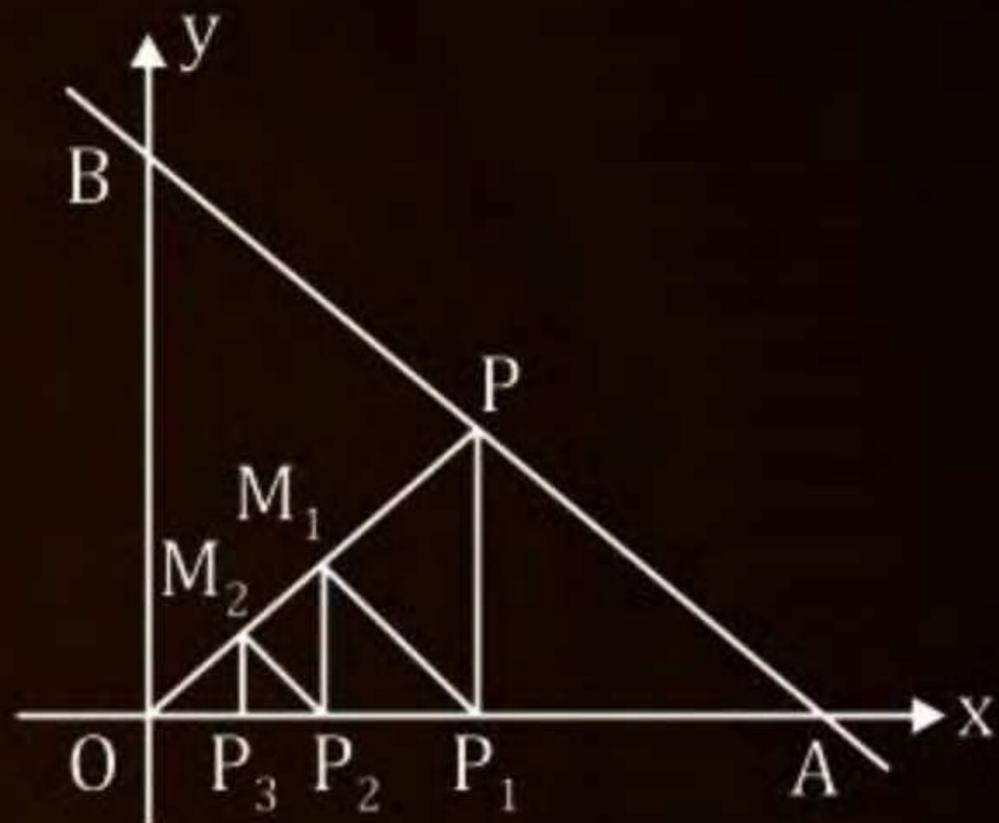
If P_n denotes the n^{th} foot of the perpendicular on OA ; then OP is

A $\left(\frac{1}{2}\right)^{n-1}$

B $\left(\frac{1}{2}\right)^n$

C $\left(\frac{1}{2}\right)^{n+1}$

D None of these



Ans. B



Homework From Module



Sequence Series:

Prarambh (Topicwise) : Complete

Prabal (JEE Main Level) : Complete

Parikshit (JEE Advanced Level) : Complete

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Revision Practice Problems (RPP)

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QUESTION

RPP 01



If a, b are the roots of $x^2 + px + 1 = 0$ and c, d are the roots of $x^2 + qx + 1 = 0$. Then find the value of $(a - c)(b - c)(a + d)(b + d)/(q^2 - p^2)$.

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Ans. 1

QUESTION

RPP 02



The least prime integral value of '2a' such that the roots α, β of the equation $2x^2 + 6x + a = 0$ satisfy the inequality $\frac{\alpha}{\beta} + \frac{\beta}{\alpha} < 2$ is

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Ans. 11



Solution to Previous TAH

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QUESTION [JEE Mains 2021 (Aug)]

Let $S_n = 1 \cdot (n - 1) + 2 \cdot (n - 2) + 3 \cdot (n - 3) + \dots + (n - 1) \cdot 1, n \geq 4$.

The sum $\sum_{n=4}^{\infty} \left(\frac{2S_n}{n!} - \frac{1}{(n-2)!} \right)$ is equal to:

A $\frac{e - 1}{3}$

B $\frac{e - 2}{6}$

C $\frac{e}{3}$

D $\frac{e}{6}$

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$(n-1) \cdot 1, n \geq 4$

The sum $\sum_{n=4}^{\infty} \left(\frac{2S_n}{n!} - \frac{1}{(n-2)!} \right)$ is equal.

$\Rightarrow T_n = n(n-1) = n^2 - n$

$\Rightarrow S_n = \sum_{n=1}^n n^2 - \sum_{n=1}^n n$
 $= \frac{n(n+1)(2n+1)}{6} - \frac{n(n+1)}{2}$
 $= \frac{n(n+1)}{2} \left[\frac{2n+1}{3} - 1 \right]$
 $= \frac{n(n+1)}{2} \left(\frac{2n-2}{3} \right) = \frac{n(n+1)(n-1)}{3}$
 $= \frac{n^3 - n}{3}$

$\sum_{n=4}^{\infty} \left(\frac{2S_n}{n!} - \frac{1}{(n-2)!} \right)$
 $\Rightarrow \sum_{n=4}^{\infty} \left(\frac{n^3 - n}{3n!} - \frac{1}{(n-2)!} \right)$
 $\Rightarrow \sum_{n=4}^{\infty} \left(\frac{n-1}{3(n-2)!} - \frac{1}{(n-2)!} \right)$
 $\Rightarrow \sum_{n=4}^{\infty} \frac{1}{3(n-3)!}$
 $\Rightarrow \frac{1}{3} \left(\frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \dots \infty \right)$
 $\Rightarrow \frac{1}{3} (e-1) \Rightarrow \frac{e-1}{3}$ Ans.

krish

Solⁿ:

$S_n = 1 \cdot (n-1) + 2 \cdot (n-2) + 3 \cdot (n-3) + \dots + (n-1) \cdot 1, n \geq 4$

$T_k = k(n-k)$
 $= nk - k^2$

$S_n = \sum_{k=1}^n T_k = n \sum_{k=1}^n k - \sum_{k=1}^n k^2$

$S_n = \frac{n(n)(n+1)}{2} - \frac{n(n+1)(2n+1)}{6}$

$\Rightarrow S_n = \frac{n(n+1)(3n-2n-1)}{6}$
 $\Rightarrow S_n = \frac{n(n+1)(n-1)}{6}$

RASIDUL

$\sum_{n=4}^{\infty} \left\{ \frac{2S_n}{n!} - \frac{1}{(n-2)!} \right\}$
 $= \sum_{n=4}^{\infty} \left\{ \frac{2n(n+1)(n-1)}{6n!} - \frac{1}{(n-2)!} \right\}$
 $= \sum_{n=4}^{\infty} \left\{ \frac{2(n+1)}{6(n-2)!} - \frac{1}{(n-2)!} \right\}$
 $= \sum_{n=4}^{\infty} \left\{ \frac{n+1-3}{3(n-2)!} \right\}$
 $= \sum_{n=4}^{\infty} \left\{ \frac{1(n-2)}{3(n-2)!} \right\}$

$= \frac{1}{3} \sum_{n=4}^{\infty} \frac{1}{(n-3)!}$
 $= \frac{1}{3} \left(\frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \dots \infty \right)$
 $= \frac{1}{3} \left(\left(\frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \dots \infty \right) - 1 \right)$
 $= \frac{e-1}{3}$

Ans: (A) $\frac{e-1}{3}$



TAH-01 $S_n = 1 \cdot (n-1) + 2 \cdot (n-2) + 3 \cdot (n-3) + \dots + (n-1) \cdot 1$

$\Rightarrow S_n = 1(n-1) + 2(n-2) + 3(n-3) + \dots + (n-1)(n-(n-1))$

$\Rightarrow S_n = [n + 2n + 3n + \dots + (n-1)n] - [1 + 4 + 9 + 16 + \dots + (n-1)^2]$

$\Rightarrow S_n = n \left[\frac{(n-1)n}{2} \right] - \frac{(n-1)n(2n-1)}{6}$

$\Rightarrow 2S_n = n^2(n-1) - \frac{n(n-1)(2n-1)}{3}$

Kritisha

$\Rightarrow \sum_{r=4}^n \left(\frac{n^2(n-1) - \frac{n(n-1)(2n-1)}{3}}{n!} \right) - \sum_{r=4}^n \frac{1}{(n-2)!}$

$\Rightarrow \sum_{r=4}^n \frac{3(n-1)}{(n-1)!} - \sum_{r=4}^n \frac{n(n-1)(2n-1)}{3(n-1)!} - \sum_{r=4}^n \frac{1}{(n-2)!}$

$\Rightarrow \sum_{r=4}^n \frac{3}{(n-2)!} - \frac{1}{3} \sum_{r=4}^n \frac{2n-1}{(n-2)!} - \sum_{r=4}^n \frac{1}{(n-2)!}$

$\Rightarrow \sum_{r=4}^n \frac{3-2+2}{(n-2)!} - \frac{1}{3} \sum_{r=4}^n \frac{2n-4+3}{(n-2)!} - \sum_{r=4}^n \frac{1}{(n-2)!}$

$\Rightarrow \sum_{r=4}^n \frac{1}{(n-3)!} + 2 \sum_{r=4}^n \frac{1}{(n-2)!} - \frac{2}{3} \sum_{r=4}^n \frac{1}{(n-3)!} - \sum_{r=4}^n \frac{1}{(n-2)!}$

$\Rightarrow \frac{1}{3} \sum_{r=4}^n \frac{1}{(n-3)!} = \frac{1}{3} \left(\frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \dots \right)$

$= \frac{1}{3} (e-1)$

$= \frac{e-1}{3} \text{ (A) Ans.}$

QUESTION



Let $f(x) = (a^2 + b^2 - 4a - 6b + 13)(2x^2 - 4x + 5)$, $a, b, x \in \mathbb{R}$ such that $f(0) = f(1) = f(2)$.
If $a, A_1, A_2, \dots, A_{10}, b$ is an arithmetic progression and $a, H_1, H_2, \dots, H_{10}, b$ is harmonic progression then the value of

$$\frac{1}{10} \left(\sum_{i=4}^8 A_i H_{11-i} \right) \text{ is equal to}$$

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Ans. 3

Tah-02

LUCKY KUMARI

$$f(x) = (a^2 + b^2 - 4a - 6b + 13)(2x^2 - 4x + 5)$$

$$f(0) = f(1)$$

$$(a^2 + b^2 - 4a - 6b + 13)(5) = (a^2 + b^2 - 4a - 6b + 13)(3)$$

$$5a^2 + 5b^2 - 20a - 30b + 65 = 3a^2 + 3b^2 - 12a - 18b + 39$$

$$2a^2 + 2b^2 - 8a - 12b + 26 = 0$$

$$a^2 + b^2 - 4a - 6b + 13 = 0$$

$$(a^2 - 4a + 4) + (b^2 - 6b + 9) = 0$$

$$(a-2)^2 + (b-3)^2 = 0$$

$$a=2 \quad \& \quad b=3.$$

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$$a, A_1, A_2, \dots, A_{10}, b \} \text{AP}$$

$$a, H_1, H_2, \dots, H_{10}, b \} \text{HP}$$

$$\text{So, } ab = A_1 H_{10} = A_2 H_9 = \dots = A_{10} H_1.$$

$$\frac{1}{10} \sum_{i=1}^{10} A_i H_{11-i} = \frac{1}{10} \left(\underbrace{A_4 H_7}_{ab} + \underbrace{A_5 H_6}_{ab} + \underbrace{A_6 H_5}_{ab} + \underbrace{A_7 H_4}_{ab} + \underbrace{A_8 H_3}_{ab} \right)$$

$$= \frac{ab \times 5}{10}$$

$$= \frac{2(3)(5)}{10} = 3.$$



Solution to **ATDB.uno** Previous KTKs

QUESTION

KTK 01



The dimensions of a Cuboid are $a > b > c$. The volume = 216 and the total outer surface area = 252. If a, b, c are in G.P., then $c =$

A 3

B 1

C 5

D 2

ATDB.uno

Ans. A



NIR-1

$a > b > c \rightarrow a, b, c$ are in H.P.

$$\text{vol.} \Rightarrow \boxed{abc = 216}$$

$$2(ab + bc + ca) = 252$$

$$\boxed{ab + bc + ca = 126}$$

$$\text{Let } a = \frac{p}{r}$$

$$b = p$$

$$c = pr$$

$$abc = p^3 = 216$$

$$\boxed{p = 6}$$

Kritisha (W.B)

$$ab + bc + ca = \frac{p^2}{r} + p^2 r + p^2$$

$$= p^2 \left(\frac{1}{r} + r + 1 \right) = 126$$

$$1 + r + \frac{1}{r} = \frac{126}{36} = \frac{7}{2}$$

$$r + \frac{1}{r} = \frac{7-2}{2} = \frac{5}{2}$$

$$r + \frac{1}{r} = \frac{5}{2}$$

$$\Rightarrow r^2 + 1 - \frac{5}{2}r = 0 \Rightarrow \boxed{2r^2 - 5r + 2 = 0}$$

$$2r^2 - 5r + 2 = 0$$

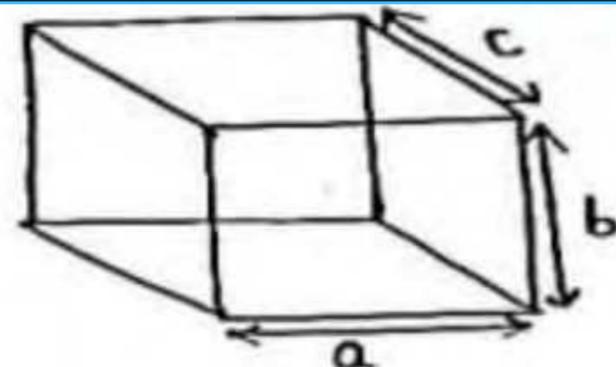
$$2r^2 - 4r - r + 2 = 0$$

$$\boxed{(2r-1)(r-2) = 0}$$

$$\rightarrow r = \frac{1}{2} \text{ as, } a > b > c$$

$$\text{They, } \boxed{c = pr = \frac{6}{2} = 3 \text{ (A)}}$$

Ans.



LUCKY KUMARI



$$\Rightarrow \text{Volume} = 216$$

$$a \times b \times c = 216$$

$$b(b^2) = 216$$

$$\boxed{b = 6}$$

$$a, b, c \text{ } \} \text{ GP}$$

$$b^2 = ac$$

$$\boxed{ac = 36}$$

$$\Rightarrow \text{Total surface S.A} = 252$$

$$2(ab + bc + ca) = 252$$

$$(ab + bc + b^2) = 126$$

$$(ca + 6c + 36) = 126$$

$$c(a + c) = 90$$

$$a + c = 15$$

$$a + \frac{36}{a} = 15$$

$$a^2 + 36 = 15a$$

$$a^2 - 12a - 3a + 36 = 0$$

$$(a - 12)(a - 3) = 0$$

$$\boxed{a = 12} \quad \& \quad a = 3$$

$$\boxed{c = 3} \quad \& \quad c = 12$$

$$\left(\text{But } a > b > c \right)$$

$$\Rightarrow a > c$$

$$\text{Hence, } \boxed{c = 3}$$



KTK-013

$a > b > c$,

Volume of a cuboid = $abc = 216$

Outer surface area of a cuboid
 $= 2(ab + bc + ca) = 252$

$\Rightarrow ab + bc + ca = 126$

$a, b, c \rightarrow$ in G.P.

Let $c \cdot r = b$

$\Rightarrow a < r < 1$ because $a > b > c$ (given)
[$r < 0$ not possible because sides are never negative]

$b = ar$
 $c = ar^2$

$\therefore abc = 216$
 $a(ar)(ar^2) = 216$

$a^3 r^3 = 216$
 $ar = 6$ $\rightarrow a = \frac{6}{r}$

$ab + bc + ca = 126$

$a(ar) + ar(ar^2) + ar^2 \cdot a = 126$

$a^2(r + r^3 + r^2) = 126$

$\frac{36}{r^2}(r^3 + r^2 + r) = 126$

$\frac{36}{r^2}(r^2 + r + 1) = 126$

$2r^2 + 2r + 2 = 7r$

$2r^2 - 5r + 2 = 0$

$2r^2 - 4r - r + 2 = 0$

$(2r - 1)(r - 2) = 0$

$r = \frac{1}{2}$, $r = 2$ X [$0 < r < 1$]
Rejected

★ KTK-1. The dimension of a cuboid are...
The volume = 216 and the total outer surface area = 252. If a, b, c are in G.P, then $c =$

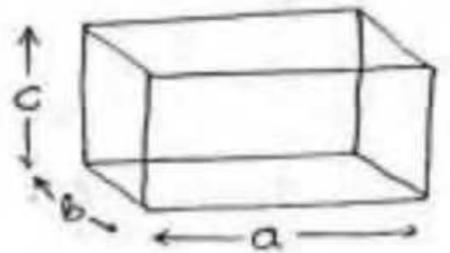
Volume = 216

$abc = 216$ — ①

T.S.A = 252

$2(ab + bc + ca) = 252$

$ab + bc + ca = 126$ — ②



Cuboid.

If a, b, c are in G.P,

then: $b^2 = ac \Rightarrow a = \frac{b^2}{c} = \frac{36}{c}$

$abc = 216$

$b^3 = 216$

$b = 6$

$6a + 6c + 36 = 126$

$6(a + c) = 90$

$a + c = 15$

$\Rightarrow \frac{36}{c} + c = 15$

$\Rightarrow 36 + c^2 = 15c$

$\Rightarrow c^2 - 15c + 36 = 0$

$\Rightarrow (c - 12)(c - 3) = 0$

$\Rightarrow c = 12$, $c = 3$
X ✓

\Rightarrow bcz given: $a > b > c$
in question & $b = 6$ then

$c = 3$ only

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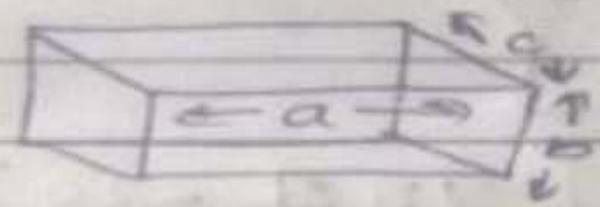
krish

KTKDL

Ankush



Solⁿ:-



∴ a, b, c are in G.P.
 $b = ar, c = ar^2$

Then, $a \cdot b \cdot c = 216$
 $a \cdot ar \cdot ar^2 = 216$
 $a^3 r^3 = 216$
 $\boxed{ar = 6}$

∴ $ab + bc + ca = 126$
 $a \cdot ar + ar \cdot ar^2 + ar^2 \cdot a = 126$
 $a^2 r + a^2 r^3 + a^2 r^2 = 126$
 $a^2 r + a^2 r^3 = 126 - 36$
 $\boxed{a^2 r + a^2 r^3 = 90}$

Volume = 216
 $a \cdot b \cdot c = 216 \quad \text{--- (i)}$

Total outer surface area = 252
 $2(ab + bc + ca) = 252$
 $ab + bc + ca = 126 \quad \text{--- (ii)}$

Now $\frac{a^2 r + a^2 r^3}{ar} = \frac{90}{6}$

$a + ar^2 = 15$
 $a(1 + r^2) = 15 \Rightarrow \frac{6}{r}(1 + r^2) = 15$
 $6 + 6r^2 = 15r \Rightarrow 2r^2 - 5r + 2 = 0$
 $(2r - 1)(r - 2) = 0 \Rightarrow r = \frac{1}{2}, r = 2$
 $r = 2$

∴ a, b, c are in G.P.
 $b^2 = ac$
 $c = \frac{b^2}{a} = \frac{a^2 r^2}{a} = \frac{36 \times 4}{6} = 24$
 $\boxed{c = 24}$

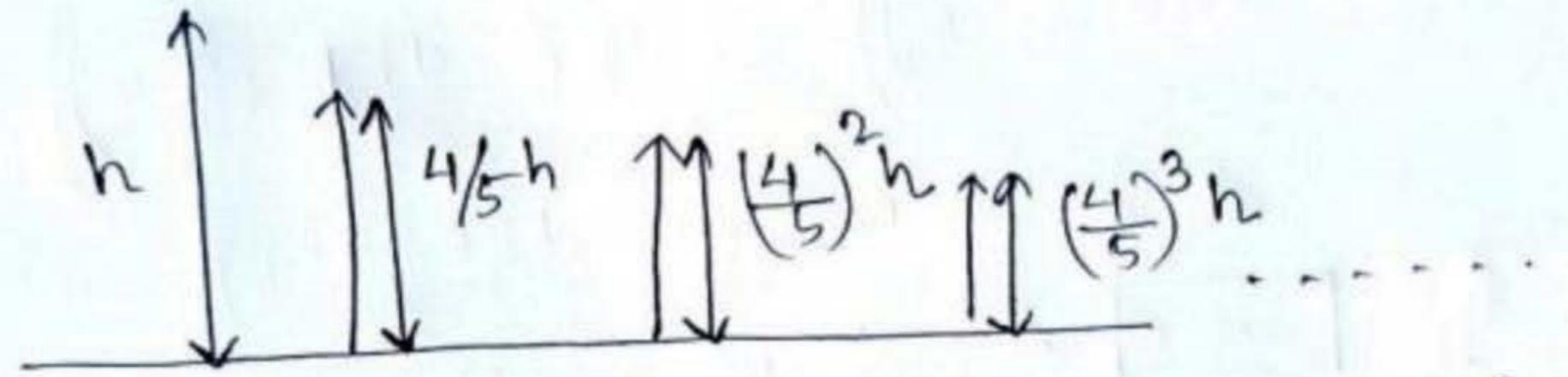
QUESTION**KTK 02**

A ball falls from a height of 100 m on a floor. If in each rebound, it describes $(4/5)^{\text{th}}$ height of the previous falling height, then the total distance travelled by the ball before it comes to rest is?

ATDB.uno**Ans. 900 m**



KTK-02



total distance travelled $(h + 2\left(\frac{4}{5}h + \left(\frac{4}{5}\right)^2 h + \left(\frac{4}{5}\right)^3 h + \dots\right))$

$= h + 2h \left(\frac{\frac{4}{5}}{1 - \frac{4}{5}}\right)$

Kritisha (W.B)

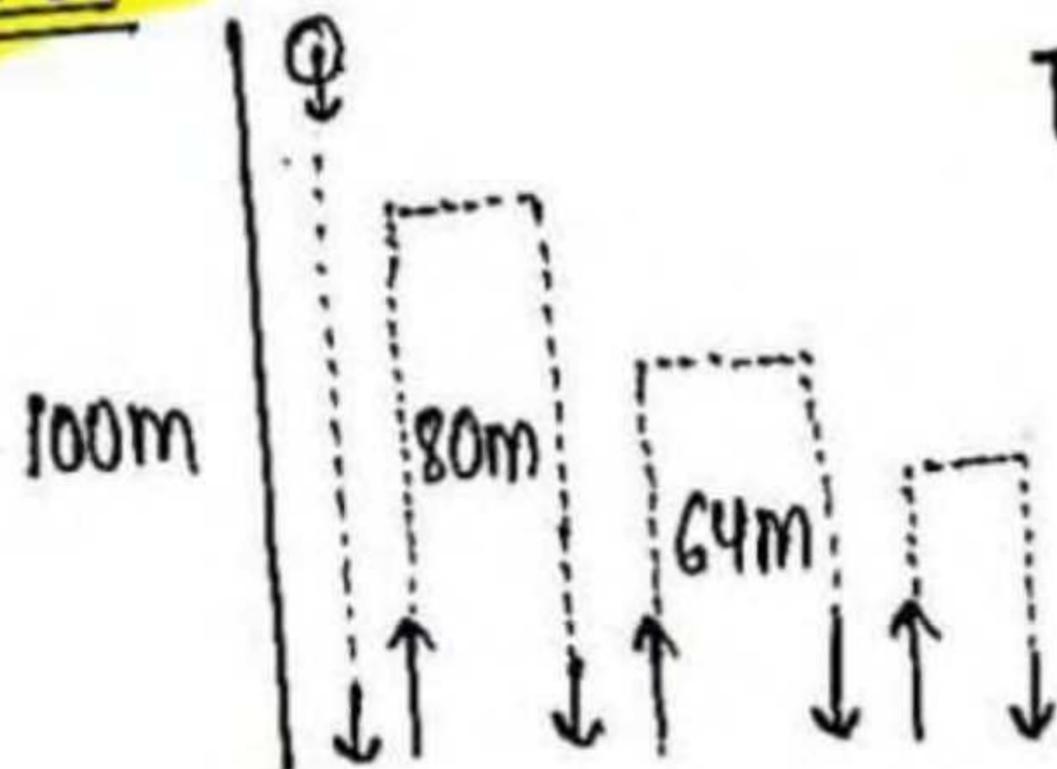
$= h + 2h \left(\frac{4}{1}\right)$

$= 9h = 900m$

LUCKY KUMARI



KTK-02



Total dist. travelled

$$= 100 + 2 \left(\frac{4}{5}(100) + \frac{4}{5} \left(\frac{4}{5} \right) (100) + \dots \infty \right)$$

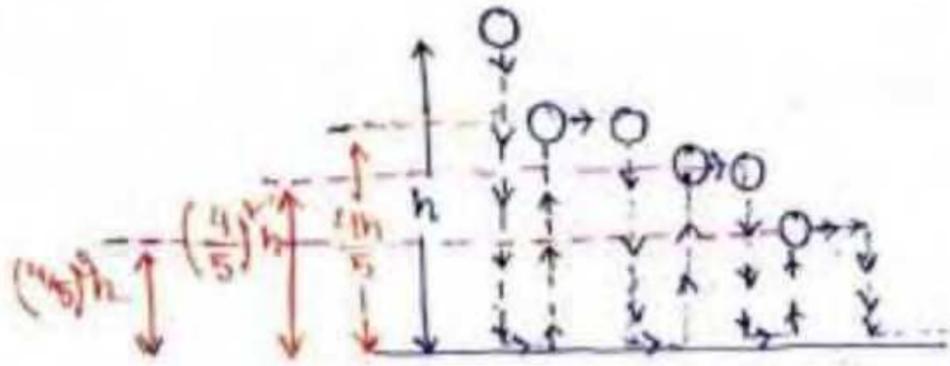
$$= 100 + 2(100) \left(\frac{4}{5} + \left(\frac{4}{5} \right)^2 + \left(\frac{4}{5} \right)^3 + \dots \infty \right)$$

$$= 100 + 200 \left(\frac{\frac{4}{5}}{1 - \frac{4}{5}} \right)$$

$$= 100 + 200(4)$$

$$= (100 + 800)m = 900m.$$

KTK-02



Total distance travelled by the ball

$$= h + \left(\frac{4h}{5} + \frac{4h}{5}\right) + \left(\left(\frac{4}{5}\right)^2 h + \left(\frac{4}{5}\right)^2 h\right) + \left(\left(\frac{4}{5}\right)^3 h + \left(\frac{4}{5}\right)^3 h\right) + \dots$$

$$= h + 2 \left[\frac{4h}{5} + \left(\frac{4}{5}\right)^2 h + \left(\frac{4}{5}\right)^3 h + \left(\frac{4}{5}\right)^4 h + \dots \infty \right]$$

$$= h + 2h \left[\left(\frac{4}{5}\right) + \left(\frac{4}{5}\right)^2 + \left(\frac{4}{5}\right)^3 + \left(\frac{4}{5}\right)^4 + \dots \infty \right]$$

$$= h + 2h \left(\frac{\frac{4}{5}}{1 - \frac{4}{5}} \right)$$

$$= h + 2h \frac{4/5}{1/5}$$

$$= h + 8h$$

$$= 9h \quad [h = 100m \text{ given}]$$

$$= 9 \times 100$$

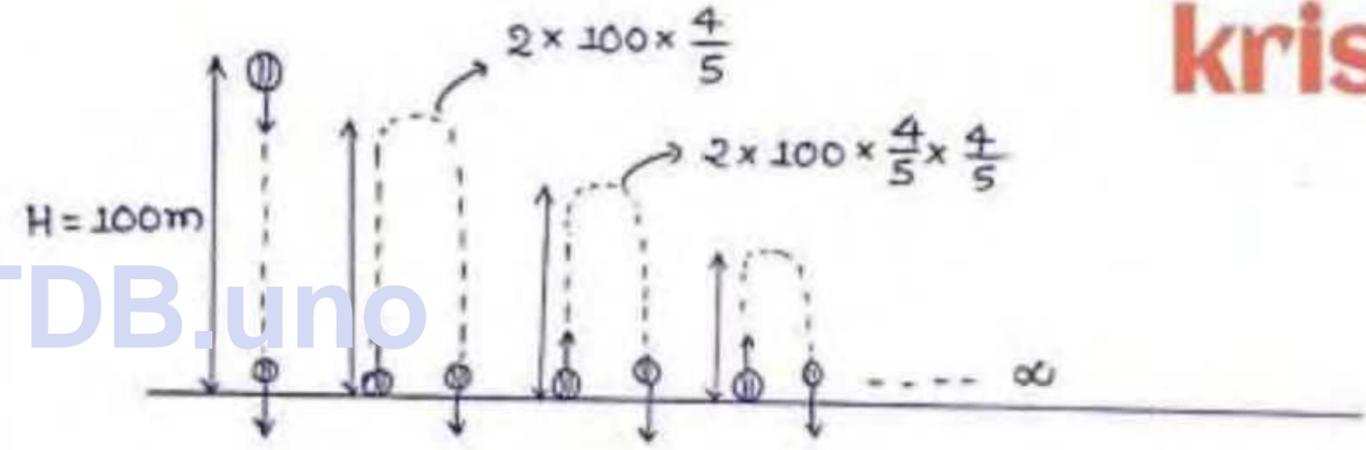
$$= 900m$$

Ans

KTK-2

A ball falls from a height 100m on a floor. If in each rebound, it describes $(4/5)^{th}$ height of previous falling height, then the total distance travelled by the ball before it comes to rest is?

krish



$$S = 100 + 2 \times 100 \times \frac{4}{5} + 2 \times 100 \left(\frac{4}{5}\right)^2 + \dots \infty$$

$$= 100 + 2 \times 100 \times \frac{4}{5} \left[1 + \frac{4}{5} + \left(\frac{4}{5}\right)^2 + \dots \infty \right]$$

$$= 100 + 160 \left[\frac{1}{1 - 4/5} \right]$$

$$= 100 + 160 \times 5$$

$$= 100 + 800 = 900m \text{ Ans}$$

QUESTION [JEE Mains 2020 (Jan)]

KTK 03



The product $2^{\frac{1}{4}} \cdot 4^{\frac{1}{16}} \cdot 8^{\frac{1}{48}} \cdot 16^{\frac{1}{128}} \dots$ to ∞ is equal to

A $2^{\frac{1}{4}}$

B $2^{\frac{1}{2}}$

C 1

D 2

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Ans. B



KTK-03

The product $2^{1/4} \cdot 4^{1/16} \cdot 8^{1/48} \cdot 16^{1/128} \dots$ to ∞ is equal to

$$\Rightarrow 2^{\frac{1}{4}} \cdot 2^{\frac{2}{16}} \cdot 2^{\frac{3}{48}} \cdot 2^{\frac{4}{128}} \dots \infty$$

$$= 2^{\frac{1}{4}} \cdot 2^{\frac{1}{8}} \cdot 2^{\frac{1}{16}} \cdot 2^{\frac{1}{32}} \dots$$

$$= 2^{\left(\frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \dots\right)}$$

$$= 2$$

$$= 2^{1/2} \text{ (B)}$$

Ans.

$$\left[\frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \dots \right]$$

$$= \frac{\frac{1}{4}}{1 - \frac{1}{2}} = \frac{\frac{1}{4}}{\frac{1}{2}}$$

$$= \frac{1}{2}$$



KTK-03

Lucky kumari

$$2^{\frac{1}{4}} \cdot 4^{\frac{1}{16}} \cdot 8^{\frac{1}{48}} \cdot 16^{\frac{1}{128}} \dots \infty$$

$$\Rightarrow 2^{\frac{1}{4}} \cdot 2^{\frac{2}{16}} \cdot 2^{\frac{3}{48}} \cdot 2^{\frac{4}{128}} \dots \infty$$

$$\Rightarrow 2^{\frac{1}{4}} \cdot 2^{\frac{1}{8}} \cdot 2^{\frac{1}{16}} \cdot 2^{\frac{1}{32}} \dots \infty$$

$$\Rightarrow 2^{\left(\frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \frac{1}{32} + \dots \infty\right)}$$

$$\Rightarrow 2^{\left(\frac{\frac{1}{4}}{1 - \frac{1}{2}}\right)} = 2 \cdot \left(\frac{1}{4}\right)^{\left(\frac{2}{1}\right)} = 2^{\frac{1}{2}}$$



KTK-3. The product of $2^{1/4} \cdot 4^{1/16} \cdot 8^{1/48} \cdot 16^{1/128} \dots$ to ∞ is

equal to :

$$\Rightarrow (2)^{1/4} \cdot (2)^{2 \times 1/16} \cdot (2)^{3 \times 1/48} \cdot (2)^{4 \times 1/128} \dots \infty$$

$$\Rightarrow 2^{1/4} \cdot 2^{1/8} \cdot 2^{1/16} \cdot 2^{1/32} \dots \infty$$

$$\Rightarrow 2^{\left(\frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \frac{1}{32} + \dots \infty \right)}$$

krish

$$\Rightarrow 2^{\left(\frac{1/4}{1 - 1/2} \right)} \Rightarrow 2^{\left(\frac{1/4}{1/2} \right)} \Rightarrow 2^{1/2} \quad \underline{\text{Ans.}}$$

QUESTION [JEE Mains 2020 (Jan)]

KTK 04



If $x = \sum_{n=0}^{\infty} (-1)^n \tan^{2n} \theta$ and $y = \sum_{n=0}^{\infty} \cos^{2n} \theta$, for $0 < \theta < \frac{\pi}{4}$, then:

A $x(1 + y) = 1$

B $y(1 - x) = 1$

C $y(1 + x) = 1$

D $x(1 - y) = 1$

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Ans. B



$$x = \sum_{n=0}^{\infty} (-1)^n \tan^{2n} \theta$$

$$= 1 - \tan^2 \theta + \tan^4 \theta - \tan^6 \theta + \tan^8 \theta - \tan^{10} \theta + \tan^{12} \theta - \tan^{14} \theta + \dots$$

$$= (1 - \tan^2 \theta) + \tan^4 \theta (1 - \tan^2 \theta) + \tan^8 \theta (1 - \tan^2 \theta) + \tan^{12} \theta (1 - \tan^2 \theta) + \dots$$

$$= (1 - \tan^2 \theta) (1 + \tan^4 \theta + \tan^8 \theta + \tan^{12} \theta + \dots)$$

$$= (1 - \tan^2 \theta) \left(\frac{1}{1 - \tan^4 \theta} \right)$$

$$x = \frac{1}{1 + \tan^2 \theta} = \frac{1}{\sec^2 \theta} = \cos^2 \theta$$

$$y = \sum_{n=0}^{\infty} \cos^{2n} \theta = 1 + \cos^2 \theta + \cos^4 \theta + \cos^6 \theta + \dots = \frac{1}{1 - \cos^2 \theta} = \frac{1}{\sin^2 \theta}$$

Hence, $x(1+y) = \cos^2 \theta \left(1 + \frac{1}{\sin^2 \theta} \right) \neq 1$

$$y(1-x) = \frac{1}{\sin^2 \theta} (1 - \cos^2 \theta) = \frac{\sin^2 \theta}{\sin^2 \theta} = 1 \quad \checkmark$$

Kritisha (W.R)

Ans.

KTK-04

LUCKY KUMARI



$$x = \sum_{n=0}^{\infty} (-1)^n \tan^{2n} \theta \quad \text{and} \quad y = \sum_{n=0}^{\infty} \cos^{2n} \theta$$

$$\Rightarrow x = 1 + (-1) \tan^2 \theta + (1) \tan^4 \theta + (-1) \tan^6 \theta + (1) \tan^8 \theta + \dots \infty$$

$$\Rightarrow x = 1 - \tan^2 \theta + \tan^4 \theta - \tan^6 \theta + \tan^8 \theta + \dots \infty$$

$$\Rightarrow x = \frac{1}{1 - (-\tan^2 \theta)} = \frac{1}{1 + \tan^2 \theta} = \frac{1}{\sec^2 \theta} = \cos^2 \theta.$$

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$$\Rightarrow y = 1 + \cos^2 \theta + \cos^4 \theta + \cos^6 \theta + \dots \infty$$

$$\Rightarrow y = \frac{1}{1 - \cos^2 \theta} = \frac{1}{\sin^2 \theta} = \operatorname{cosec}^2 \theta.$$

option (A). $x(1+y) = \cos^2 \theta (1 + \operatorname{cosec}^2 \theta)$

$$= \frac{\cos^2 \theta (\sin^2 \theta + 1)}{\sin^2 \theta}$$

$$= \cot^2 \theta (\sin^2 \theta + 1)$$

$$\neq \text{RHS.}$$

option (B). $y(1-x) = \operatorname{cosec}^2 \theta (1 - \cos^2 \theta)$

$$= \operatorname{cosec}^2 \theta (\sin^2 \theta)$$

$$= \frac{1}{\sin^2 \theta} \cdot \sin^2 \theta$$

$$= 1 = \text{RHS.}$$



PROVE:

$$\text{If } x = \sum_{n=0}^{\infty} (-1)^n \tan^{2n} \theta \quad \& \quad y = \sum_{n=0}^{\infty} \cos^{2n} \theta,$$

for $0 < \theta < \frac{\pi}{4}$ then :

$$\# \quad x = \sum_{n=0}^{\infty} (-1)^n \tan^{2n} \theta$$

$$x = 1 - \tan^2 \theta + \tan^4 \theta - \tan^6 \theta + \dots \infty$$

$$= \frac{1}{1 - (-\tan^2 \theta)} = \frac{1}{1 + \tan^2 \theta}$$

$$= \frac{1}{\sec^2 \theta} = \cos^2 \theta.$$

$$\# \quad y = \sum_{n=0}^{\infty} \cos^{2n} \theta$$

$$y = 1 + \cos^2 \theta + \cos^4 \theta + \dots + \infty$$

$$= \frac{1}{1 - \cos^2 \theta}$$

krishh

$$\Rightarrow y = \frac{1}{1-x} \quad \because \text{ } x = \cos^2 \theta$$

$$\Rightarrow y - xy = 1$$

$$\Rightarrow y(1-x) = 1 \quad \text{Ans.}$$

QUESTION [JEE Mains 2024 (1 Feb)]

KTK 05



Let S_n denote the sum of first n terms of an arithmetic progression. If $S_{10} = 390$ and the ratio of the tenth and the fifth terms is $15 : 7$, then $S_{15} - S_5$ is equal to:

A 800

B 890

C 790

D 690

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Ans. C

$$S_{10} = 5(2a + 9d) = 390$$

$$2a + 9d = 78$$

Kritisha (W.B)

$$\frac{a_{10}}{a_5} = \frac{15}{7}$$

$$\frac{a+9d}{a+4d} = \frac{15}{7} \Rightarrow$$

$$\left(\frac{a+9d + a+4d}{5d} = \frac{22}{8} \right)$$

$$\Rightarrow \frac{78+4d}{5d} = \frac{11}{4}$$

$$\Rightarrow 4(78+4d) = 55d$$

$$\Rightarrow 312 = (55-16)d$$

$$\Rightarrow \boxed{d = \frac{312}{39} = 8} ; 2a = 78 - 72$$

$$\boxed{a = 3}$$

$$S_{15} - S_5 = \frac{15}{2}(2a + 14d) - \frac{5}{2}(2a + 4d)$$

$$= \frac{15}{2}(6 + 112) - \frac{5}{2}(6 + 32)$$

$$= \frac{15}{2}(118) - \frac{5}{2}(38)$$

$$= (15 \times 59) - (5 \times 19)$$

$$= 885 - 95 = \underline{\underline{790(c)}}$$



LUCKY KOMARI



KTK-05

$$S_{10} = 390$$

$$\Rightarrow \cancel{10} \left[\frac{2a+9d}{2} \right] = \cancel{390} \cdot 78$$

$$\Rightarrow 2a + 9d = 78 \quad \text{--- (I)}$$

$$\frac{T_{10}}{T_5} = \frac{15}{7}$$

$$\Rightarrow \frac{a+9d}{a+4d} = \frac{15}{7}$$

$$\Rightarrow 7a + 63d = 15a + 60d$$

$$\Rightarrow 3d = 8a$$

$$\Rightarrow \boxed{2a = \frac{3d}{4}} \quad \text{--- (II)}$$

from (I) & (II)

$$\frac{3d}{4} + 9d = 78$$

$$35d = \frac{2}{78} (4)$$

$$\boxed{d = 8}$$

$$\boxed{a = 3}$$

Now,

$$S_{15} - S_5$$

$$\frac{15}{2} [2a + 14d] - \frac{5}{2} [2a + 4d]$$

$$\Rightarrow 15(a + 7d) - 5(a + 2d)$$

$$\Rightarrow 10a + 95d$$

$$\Rightarrow 10(3) + 95(8)$$

$$= 30 + 760 = 790.$$

KTK-5.

Let S_n denote the sum of first n terms of an arithmetic progression. If $S_{10} = 390$ & the ratio of the tenth and the fifth term is $15:7$, then $S_{15} - S_5$ is equal to:

$$\Rightarrow S_{10} = 390$$

$$\Rightarrow 5 \frac{10}{2} [2a + 9d] = 390$$

$$\Rightarrow 2a + 9d = 78 \text{ --- (1)}$$

$$\Rightarrow 2 \left(\frac{3d}{4} \right) + 9d = 78$$

$$\Rightarrow 3d + 36d = 78 \times 4$$

$$\Rightarrow 39d = 78 \times 4$$

$$\boxed{d=8}$$

$$\Rightarrow \frac{a_{10}}{a_5} = \frac{15}{7}$$

$$\Rightarrow \frac{a+9d}{a+4d} = \frac{15}{7}$$

$$\Rightarrow 7a + 63d = 15a + 60d$$

$$\Rightarrow 8a = 3d \Rightarrow a = \frac{3d}{8}$$

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$$\Rightarrow a = \frac{3 \times 8}{8} \Rightarrow \boxed{a=3}$$

$$\# \text{ find : } S_{15} - S_5$$

$$\Rightarrow \frac{15}{2} [2a + 14d] - \frac{5}{2} [2a + 4d]$$

$$\Rightarrow 15a + 105d - 5a - 10d$$

$$\Rightarrow 10a + 95d$$

$$\Rightarrow 30 + 760$$

$$\Rightarrow 790 \text{ Ans.}$$

krish





Solution to Previous RPPs

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QUESTION

(RPP 1)



Paragraph

Consider the quadratic equation $2x^2 - (4m + 2)x + m^2 + m = 0, m \in \mathbb{R}$

1. The number of positive integer values of 'm' such that the equation has exactly one root in (2, 3) is

(A) 3

(B) 4

(C) 5

(D) 6

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2. The number of negative integral values of 'm' such that $m > -10$ and at least one root of the equation is smaller than '2' is

(A) 8

(B) 9

(C) 6

(D) 4

Ans. (1) B, (2) B

QUESTION

(Challenger Problem (Answers Sahi hai))



If $ax^2 + bx + c = 0$, $a \neq 0$, $a, b, c \in \mathbb{R}$ has two distinct real roots in $(1, 2)$ then

RPP 02

- A** (a) $(5a + 2b + c) > 0$
- B** (a) $(5a + 2b + c) < 0$
- C** $2a + b > 0$
- D** (a) $(4a + 2b + c) > 0$

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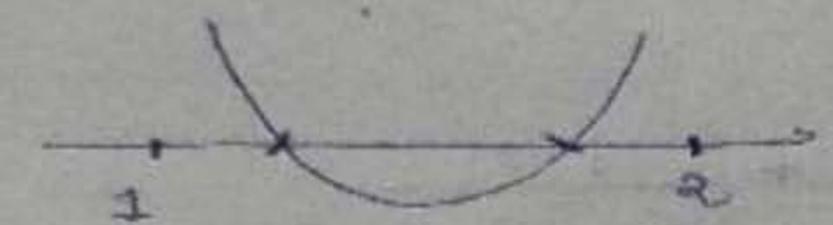
Ans. A, D



RPP-1

If $ax^2+bx+c=0$, $a \neq 0$, $a, b, c \in \mathbb{R}$ has two distinct roots in $(1, 2)$ then

Solⁿ



$$1 < -\frac{b}{2a} < 2 \quad \text{--- (i)}$$

$$a \cdot f(1) > 0 \quad \text{--- (ii)}$$

$$a \cdot f(2) > 0 \quad \text{--- (iii)}$$

$a \cdot f(2) > 0$

$a \cdot (4a+2b+c) > 0 \Rightarrow \textcircled{D}$

$1 < -\frac{b}{2a} < 2$

$$\Rightarrow \left. \begin{matrix} 1 < -\frac{b}{2a} \\ 2a+b < 0 \end{matrix} \right\} \begin{matrix} -\frac{b}{2a} < 2 \\ 0 < 4a+b \end{matrix}$$

In option - A

$(a) (a+4a+2bc)$

$a^2+a(4a+2b+c)$

$$\downarrow > 0 \quad \downarrow > 0$$

always ≥ 0

\textcircled{A} & \textcircled{D}

ADRISH SIL FROM WEST BENGAL HOOGH



THANK ATDB.uno YOU